

GRAPH

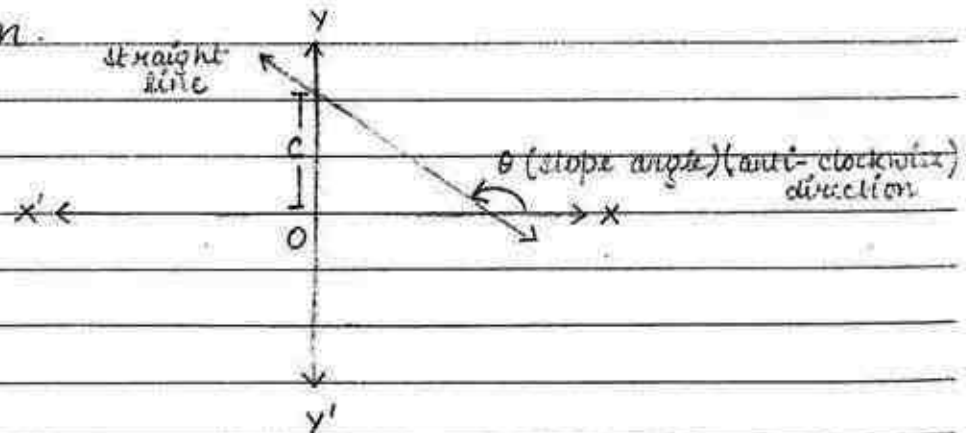
definition: It is a diagrammatic representation of data physical relation between two physical quantities is called graph.

1 Straight line

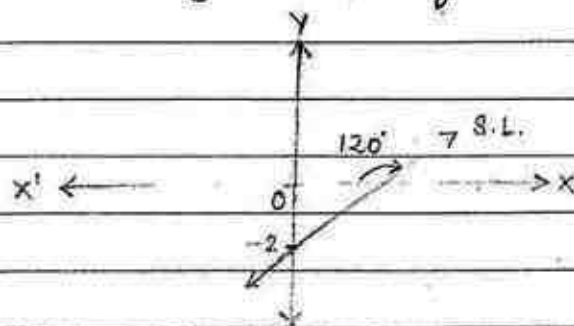
standard form of straight line:

$y = mx + c$, where x and y are two physical quantities; $m = \text{slope}$ and $\text{slope} = \tan \theta$; $c = \text{intercept on } y \text{ axis}$, where θ is a slope angle

Slope angle(θ): It is the angle made by straight line with x -axis in anti-clockwise direction.



Q.1 For given, straight line, find the following:

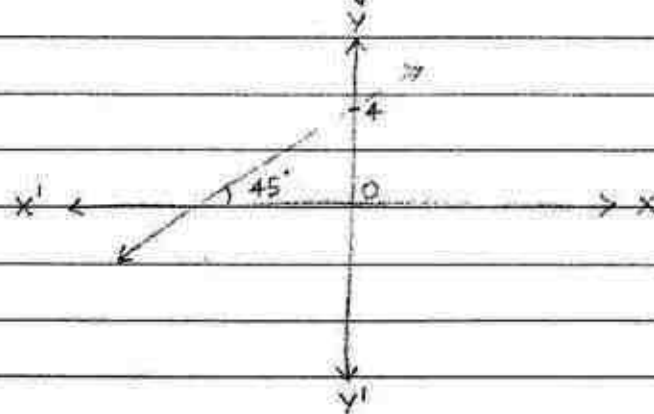


- i) Slope angle (θ) : $(180^\circ - 120^\circ) = 60^\circ$
- ii) Slope (m) : $\tan \theta = \tan 60^\circ = \sqrt{3}$
- iii) c (intercept) : -2
- iv) eq of straight line : $y = mx + c$

$$y = \sqrt{3}x + (-2)$$

$$y = \sqrt{3}x - 2$$

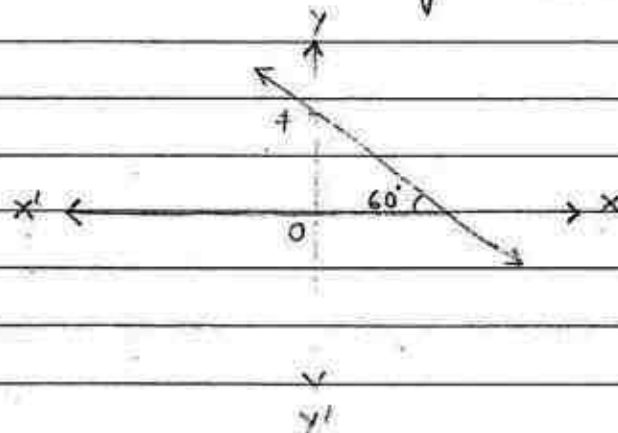
Q.2



Find the following:

- i) slope angle (θ) : 45°
 - ii) slope (m) : $\tan 45^\circ = 1$
 - iii) c (intercept) : 4
 - iv) eq of straight line : $y = mx + c$
- $$y = x + 4$$

Q.3



Find the following:

- i) slope angle (θ) : $(180^\circ - 60^\circ) = 120^\circ$
- ii) slope (m) : $\tan 120^\circ = \tan (180^\circ - 60^\circ) = -\tan 60^\circ$
 $= -\sqrt{3}$

iii) c (intercept) : +

iv) eq. of straight line : $y = mx + c$
 $- \sqrt{3}x + 4$

Possible value of slope ($\tan \theta$) :

~~If~~ slope = $m = \tan \theta$

If

• $m = +ve$ or $\tan \theta = +ve$

then $\theta < 90^\circ$ i.e. acute angle.

• $m = -ve$ or $\tan \theta = -ve$

then $90^\circ < \theta < 180^\circ$ i.e. obtuse angle

• $m = 0$ or $\tan \theta = 0$

i.e. $\theta = 0^\circ$, then straight line will be parallel to x-axis

• $m = \infty$ or $\tan \theta = \infty$

i.e. $\theta = 90^\circ$, then straight line will be parallel to y-axis.

Possible value of c (intercept)

If

• $c = +ve$

then straight line cuts the y-axis above the origin.

• $c = -ve$

then straight line cuts the y-axis below the origin.

• $c = 0$

then straight line passes through origin

Q.4. For the given equation of the straight line find, slope (m), slope angle (θ), c , draw the straight line

$$y = \sqrt{3}x - 4$$

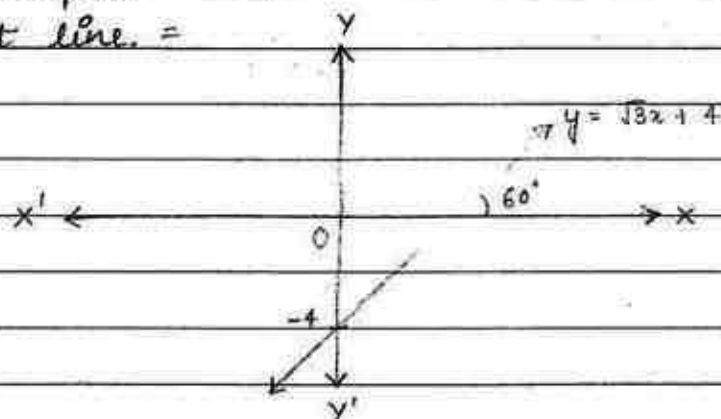
i) Slope (m) = $\sqrt{3}$

ii) Slope angle (θ) = $\tan \theta = \sqrt{3}$

$$\therefore \theta = 60^\circ$$

iii) c (intercept) = -4

iv) Straight line =



Q.5. $3y = -\sqrt{3}x - 9$

For the given equation of the straight line find the following

$$y = \frac{-\sqrt{3}x - 9}{3}$$

$$y = \frac{-1}{\sqrt{3}}x - 3$$

i) Slope (m) = $-\frac{1}{\sqrt{3}}$

ii) Slope angle (θ) = $\tan \theta = -\frac{1}{\sqrt{3}}$

[$\because \theta$ is -ve \therefore angle lies between 90° and 180°]

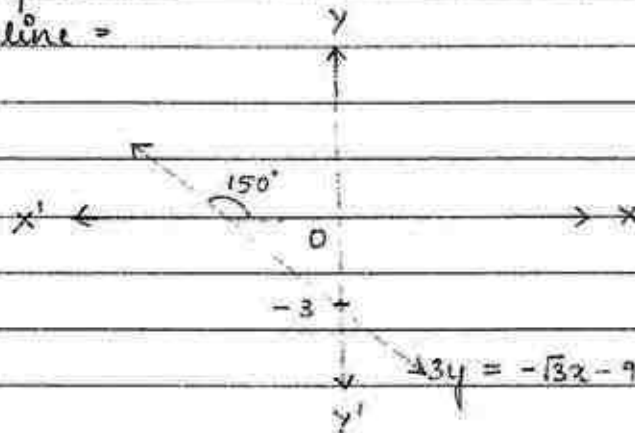
$$\tan(180^\circ - 30^\circ) = -\tan 30^\circ$$

$$\tan 150^\circ = \frac{-1}{\sqrt{3}} = \tan \theta.$$

$$\therefore \theta = 150^\circ$$

iii) C (intercept) = -3

iv) straight line =



Trigonometrical Inverse function:

For finding angle θ

i) $\sin \theta = \frac{\sqrt{3}}{2}$

$$\therefore \theta = \sin^{-1}\left(\frac{\sqrt{3}}{2}\right)$$

$$\therefore \theta = 60^\circ$$

ii) $\tan \theta = 1$

$$\therefore \theta = \sin^{-1}(1)$$

$$\therefore \theta = 45^\circ$$

iii) $\tan \theta = \frac{16}{5}$

$$\therefore \theta = \tan^{-1}\left(\frac{16}{5}\right)$$

$$(v) \quad \sin \theta = \frac{5}{6}$$

$$\therefore \theta = \sin^{-1} \left(\frac{5}{6} \right)$$

Q.6

$$5y + 7x - 10 = 0$$

Find the following for the given equation of straight line

$$5y = -7x + 10$$

$$\therefore y = \frac{-7x + 10}{5}$$

$$\therefore y = \frac{-7x}{5} + 2$$

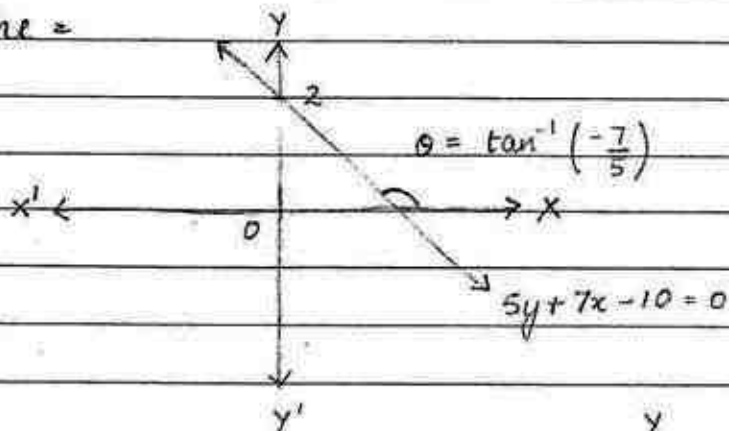
i) slope (m) = $-\frac{7}{5}$

ii) slope angle (θ) = $\tan \theta = -\frac{7}{5}$

$$\therefore \theta = \tan^{-1} \left(-\frac{7}{5} \right)$$

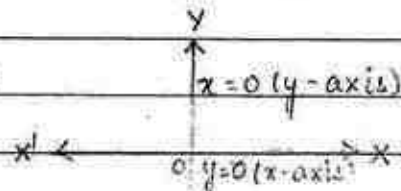
(iii) Intercept (c) = 2

(iv) straight line =



• equation of x-axis is $y = 0$

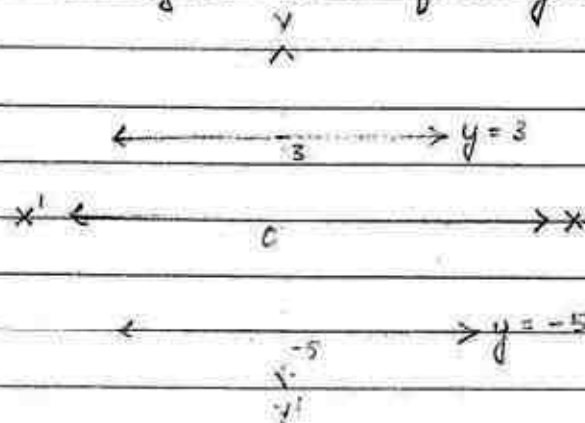
• equation of y-axis is $x = 0$



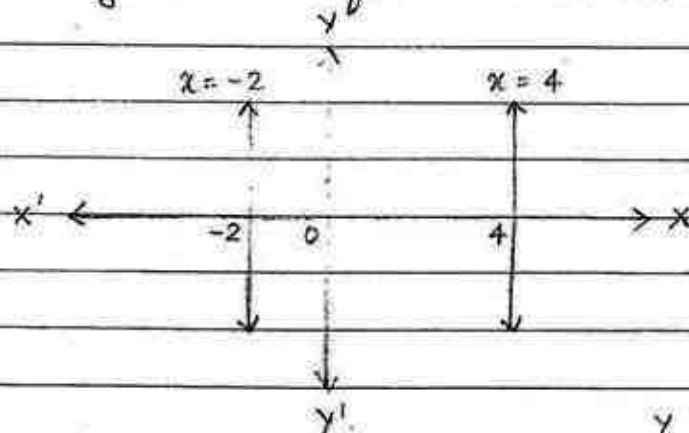
- If $y = \text{constant}$
then straight line will be \perp to y -axis or parallel to x -axis

- If $x = \text{constant}$
then straight line will be \perp to x -axis or parallel to y -axis

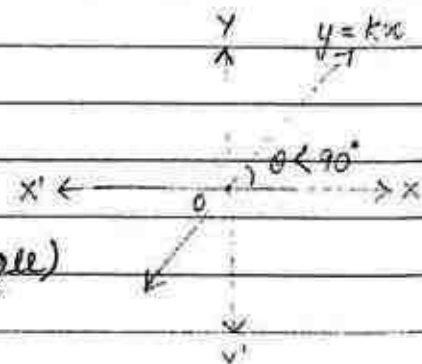
Q.7. Draw the straight line for $y = 3$ and $y = -5$



Q.8. Draw the straight line for $x = 4$ and $x = -2$



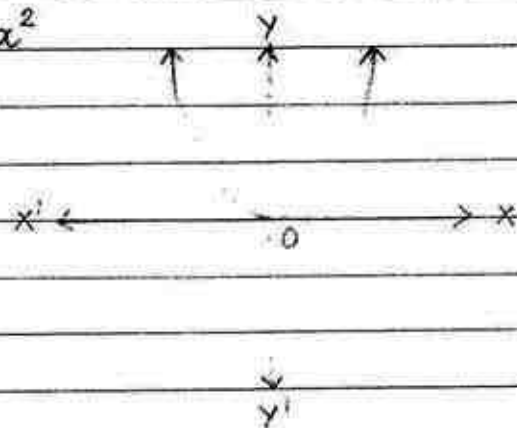
- If $y \propto x$
 $y = kx$ (k is constant)
 $\therefore y = kx + 0$
 $m = +k$ ($+$ implies acute angle)
 $\therefore \theta < 90^\circ$



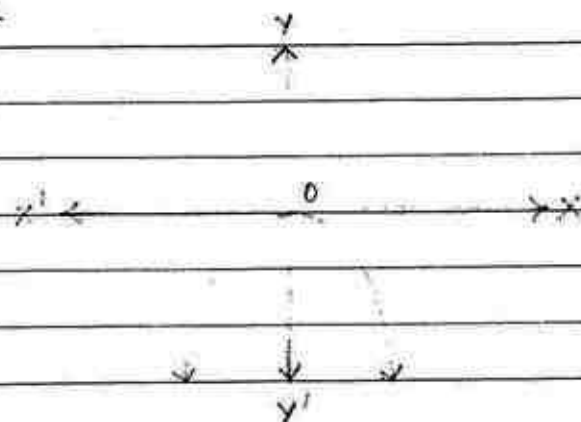
2. Parabola

There are four types of Parabolic graph.

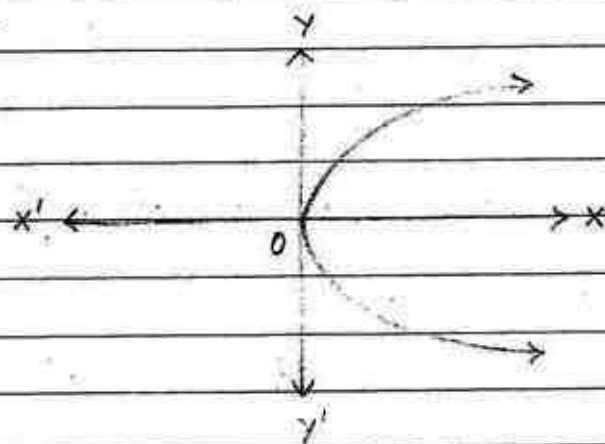
i) $y = kx^2$



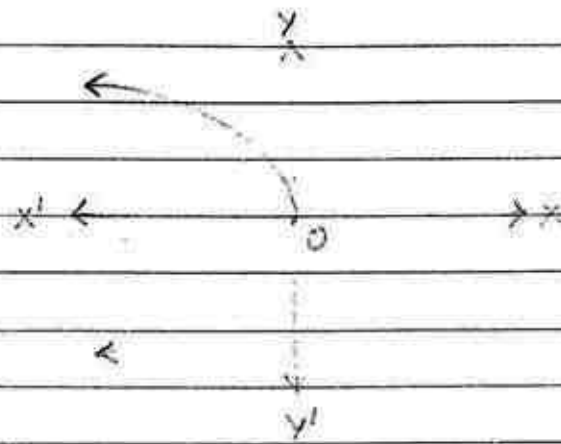
ii) $y = -kx^2$



iii) $x = ky^2$

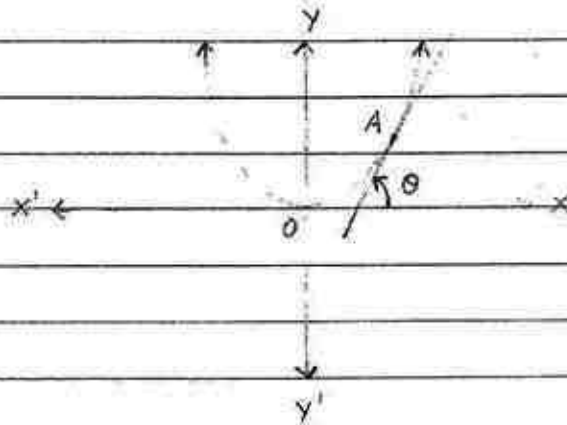


iv) $x = -ky^2$



Parabola always bends towards that variable whose power is smaller.

Slope:



$$[\text{slope}]_A : \tan \theta$$

To find slope at any point on a graph:

- Draw a tangent at a given point on a graph.
- Let θ is the angle made by tangent with x-axis in anticlockwise direction.
- The value of $\tan \theta$ will be slope of that graph at that particular point.

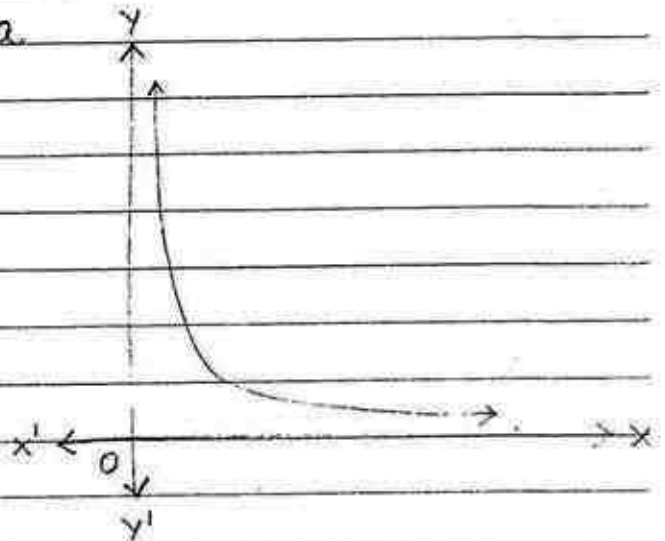
2.3. Rectangular hyperbola

$$y \propto \frac{1}{x}$$

$$y = \frac{k}{x}$$

$$xy = k$$

$$xy = \text{constant}$$



- If $x = 0$,

$$\text{then } y = \frac{k}{x} = \frac{k}{0} = \infty$$

- If $x = 1$

$$\text{then } y = \frac{k}{1} = k$$

- If $x = 2$

$$\text{then } y = \frac{k}{x} = \frac{k}{2}$$

- If $x = 10$

$$\text{then } y = \frac{k}{x} = \frac{k}{10}$$

- If $x = \infty$

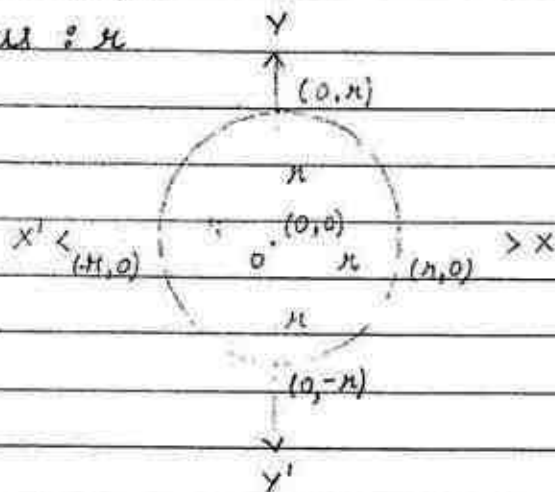
$$\text{then } y = \frac{k}{x} = \frac{k}{\infty} = 0$$

4. Circle :

Standard equation : $x^2 + y^2 = r^2$

Centre : $(0, 0)$

radius : r



Q.9.

For a given equation of circle $x^2 + y^2 = 5$.

$$x^2 + y^2 = r^2 = 5 = (\sqrt{5})^2$$

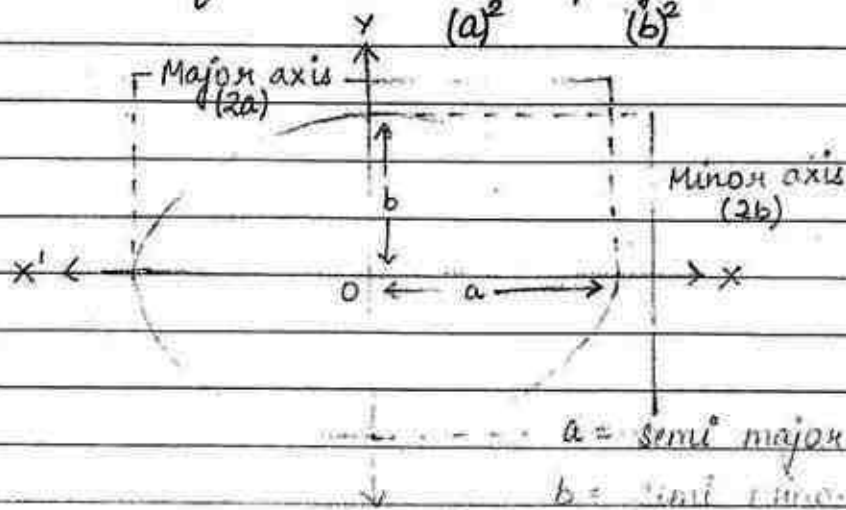
\therefore centre = $(0, 0)$.

radius = $\sqrt{5}$

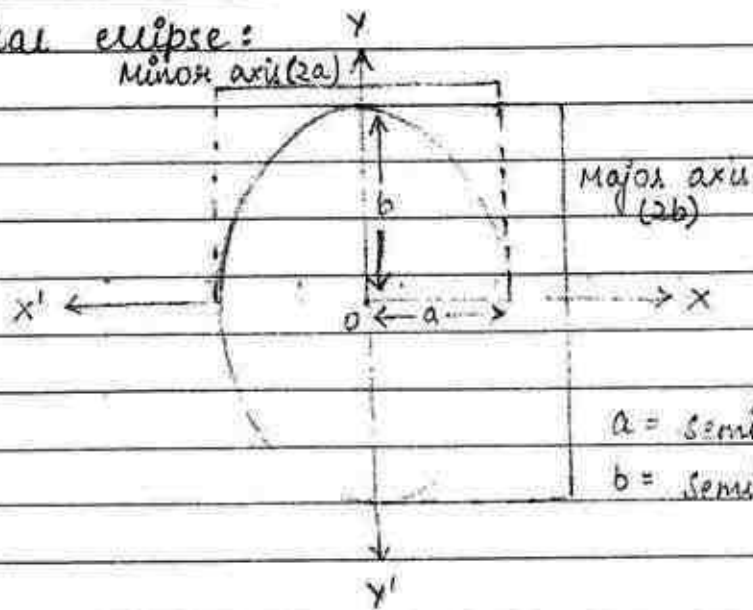
5. Ellipse :

i) Horizontal ellipse

Standard equation : $\frac{x^2}{(a)^2} + \frac{y^2}{(b)^2} = 1$



ii) Vertical ellipse:



• If $a = b$, then ellipse is converted into circle.

$$\frac{x^2}{a^2} + \frac{y^2}{a^2} = 1$$

$$x^2 + y^2 = (a)^2$$

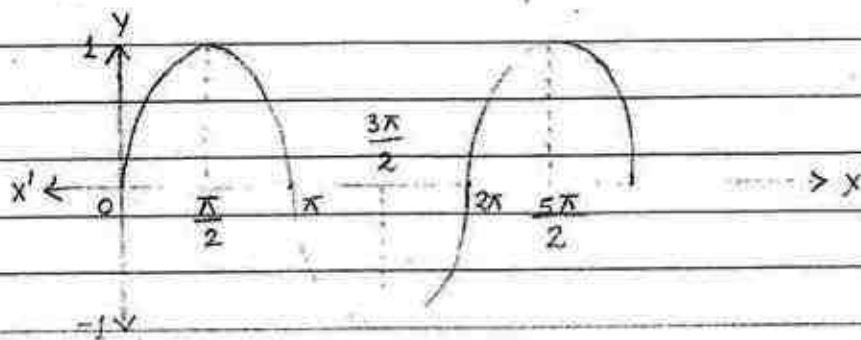
$\therefore x^2 + y^2 = (r)^2$ Hence, it is circle.

6. Graph of Trigonometrical function:

i) sine curve (graph on sine graph) (sine view)

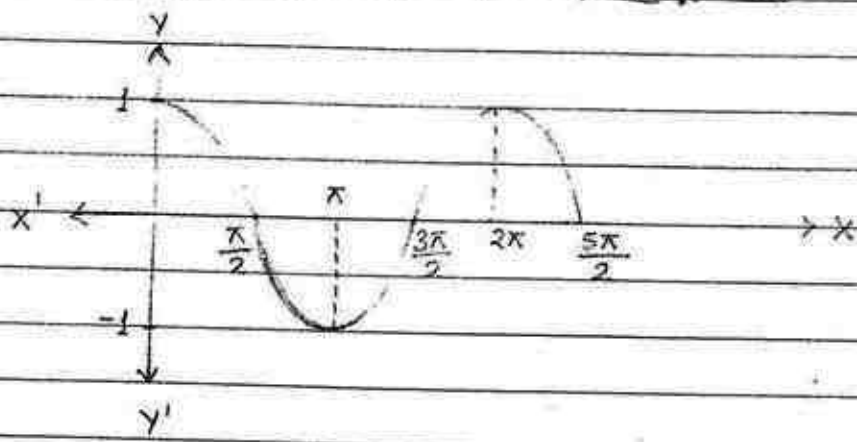
$$y = \sin(x)$$

y	0	1	0	-1	0	1	0
x	0	$\pi/2$	π	$3\pi/2$	2π	$5\pi/2$	3π



- Sine $(0, \pi, 2\pi, 3\pi, 4\pi \dots) = 0$.
- Minimum value: -1 and Maximum value: 1
- ii) Cosine curve (graph on cos graph).
 $y = \cos(x)$

y	1	0	-1	0	1	0	-1
x	0	$\pi/2$	π	$3\pi/2$	2π	$5\pi/2$	3π



- Maximum value for cos: 1
Minimum value for cos: -1
- $\cos\left(\frac{\pi}{2}, \frac{3\pi}{2}, \frac{5\pi}{2}, \frac{7\pi}{2} \dots\right) = 0$

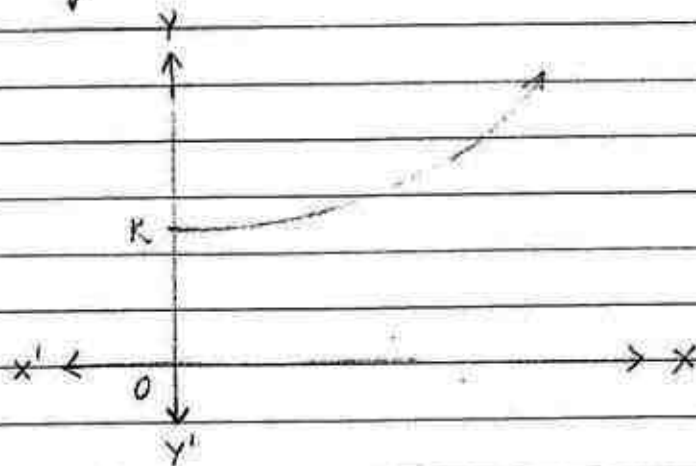
7. Exponential graph

i) Exponential graph growth graph

$$y = ke^x$$

- $1^\infty = 1$
 $2^\infty = \infty$
 $e^\infty = \infty$ } value of $e = 2.718$

- If $x = 0$
then $y = ke^0 = k$
- If $x = 1$
then $y = ke^1 = ke$
- If $x = 2$
then $y = ke^2$
- If $x = 10$
then $y = ke^{10}$
- If $x = \infty$
then $y = ke^\infty = k\infty = \infty$



ii) Exponential decay graph.

$$y = ke^{-x}$$

- If $x = 0$,
then $y = ke^0 = k$

• If $x = 1$
then $y = ke^{-1} = \frac{k}{e}$

• If $x = 2$
then $y = ke^{-2} = \frac{k}{e^2}$

• If $x = 10$
then $y = ke^{-10} = \frac{k}{e^{10}}$

• If $x = \infty$
then $y = \frac{ke^{-\infty}}{e^{\infty}} = \frac{k}{\infty} = 0$

