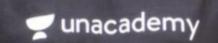
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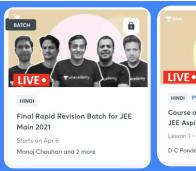
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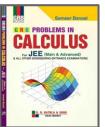


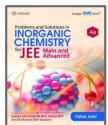




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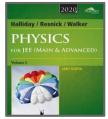


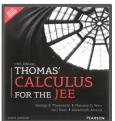








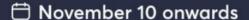






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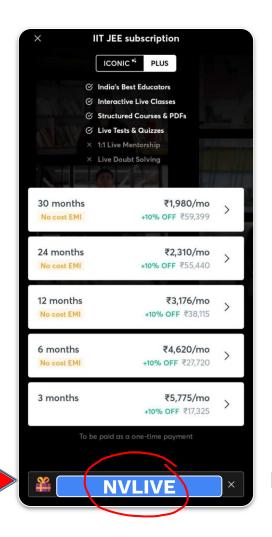
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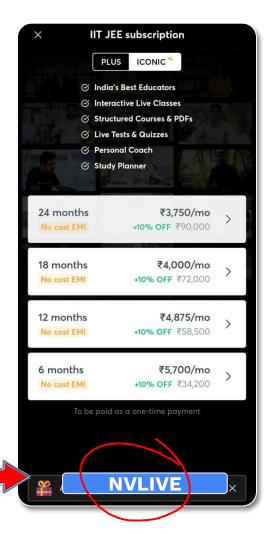


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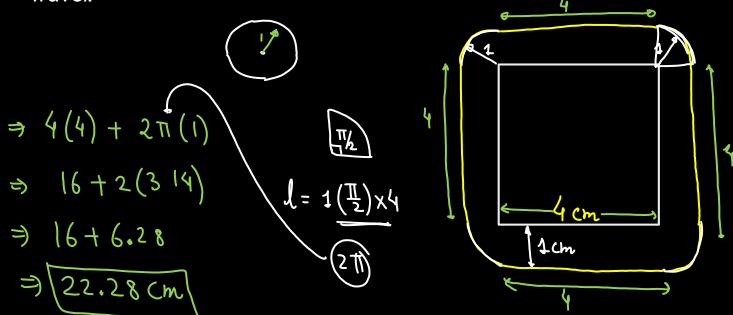
QUESTIONS





Q

Consider a square of side 4 cm. Now if a man runs at a distance of 1 cm from the sides of the square. How much distance will he travel.







Let $f_k(x) = \frac{1}{k} \left(\sin^k x + \cos^k x \right)$ where $x \in R$ and $k \ge 1$.

Let
$$f_k(x) = \frac{1}{k} (\sin^k x + \cos^k x)$$
 where $x \in R$ and $k \ge 1$.
Then $f_4(x) - f_6(x)$ equals $\frac{1}{4} - \frac{1}{6}$

(a)
$$\frac{1}{4}$$
 (b) $\frac{1}{12}$ (c) $\frac{1}{6}$ (d) $\frac{1}{3}$ [JEE M 2014]
$$f_4(\pi) - f_6(\pi)$$

$$\Rightarrow \bot (Au'(\pi) + (au'(\pi)) + \bot (Au'(\pi) + (au'(\pi)))$$

$$\Rightarrow \bot (Au'(\pi) + (au'(\pi)) + \bot (Au'(\pi) + (au'(\pi)))$$

$$\frac{f_4(n) - f_6(n)}{4\left(\sin^4 n + \cos^4 n\right) - \frac{1}{6}\left(\sin^6 n + \cos^6 n\right)} = \frac{\# \text{NVStyle}}{f_k(n)} = \frac{1}{k}(1) = \frac{1}{k}$$

$$\frac{1}{4}\left(1 - 2\sin^2 n\right) - \frac{1}{6}\left(1 - 3\sin^2 n\cos^2 n\right) = \frac{1}{k}(1) = \frac{1}{k}$$

(a)
$$\frac{1}{4}$$
 (b) $\frac{1}{12}$ (c) $\frac{1}{6}$ (d) $\frac{1}{3}$ [JEE M 2014]
$$\begin{cases}
\frac{1}{4}(\pi) - \frac{1}{6}(\pi) \\
\frac{1}{4}(\pi) - \frac{1}{6}(\pi)
\end{cases}$$

$$\Rightarrow \frac{1}{4}(\frac{1}{4}(\pi) + \frac{1}{6}(\pi)) - \frac{1}{6}(\frac{1}{4}(\pi) + \frac{1}{6}(\pi)) + \frac{1}{6}(\pi) = \frac{1}{6}(\pi)$$

For any $\theta \in \left(\frac{\pi}{4}, \frac{\pi}{2}\right)$ the expression

$$3(\sin\theta - \cos\theta)^4 + 6(\sin\theta + \cos\theta)^2 + 4\sin^6\theta \text{ equals:}$$

(b)
$$13 - 4\cos^{6}\theta$$

(c) $13 - 4\cos^{2}\theta + 6\cos^{4}\theta$

(c)
$$13 - 4\cos^2\theta + 6\cos^4\theta$$

(d) $13 - 4\cos^4\theta + 2\sin^2\theta\cos^4\theta$

(c)
$$13 - 4\cos^2\theta + 6\cos^2\theta$$

(d) $13 - 4\cos^4\theta + 2\sin^2\theta$

(d)
$$13 - 4\cos^4\theta + 2\sin^2\theta$$

$$3(s-c)^{4}+6(s+c)^{2}+$$

$$3(s-c)^{4}+6(s+c)^{2}+4s^{6}$$

$$=3(1-2sc)^{2}+6(1+2sc)+4(1-c^{2})^{3}$$

(c)
$$13 - 4\cos^2\theta + 6\cos^4\theta$$

(d) $13 - 4\cos^4\theta + 2\sin^2\theta\cos^2\theta$

$$13 - 4\cos^2\theta + 6\sin^2\theta\cos^2\theta$$

$$13 - 4\cos^6\theta$$

$$13 - 4\cos^2\theta + 6\cos^4\theta$$

= 3(1+482c2-48c)+6+128c+4(1-66-8c2(1-c2))

$$6\cos^4\theta$$



$$= 3 + 12 5^{2} c^{2} - 128c + 6 + 128c + 4 - 46^{6} - 12c^{2} + 12c^{4}$$

$$= 3 + 12c^{2}(1-c^{2}) + 10 - 4c^{6} - 12c^{2} + 12c^{4}$$

$$= 13 - 4 \cos \theta$$



If $15 \sin^4 \alpha + 10 \cos^4 \alpha = 6$, for some $\alpha \in R$,

then the value of
$$27 \sec^6 \alpha + 8 \csc^6 \alpha$$
 is

$$|S(4m^{2}x)^{2} + |O(cos^{2}x)|^{2} = 6$$

$$\Rightarrow |S(t)^{2} + |O(1-t)^{2} = 6$$

$$\Rightarrow |St^{2} + |O(1+t^{2}-2t)| = 6$$

$$\Rightarrow |St^{2} + |O(1+t^{2}-2t)| = 6$$

$$\Rightarrow |St^{2} - 20t + |4| = 8$$



$$\tan^2 x = \frac{2}{3}$$

 $\sin^4 x$

If

$$\tan^2 x = \frac{1}{3}$$

 $\cos^4 x$

$$\tan^2 x = \frac{1}{3}$$

$$\tan^2 x = \frac{1}{3}$$

$$\left(\sin^2 x \right)^2 \quad \left(\cos^2 x \right)^{-\frac{1}{3}}$$

$$\tan^2 x = \frac{1}{3}$$

$$(4m^2n)^2 \qquad (6.2)^2$$

$$\tan^2 x = \frac{1}{3}$$

$$\left(\cos^2 x \right)$$

$$\frac{\sin^8}{8}$$

MCO

then

$$\frac{27}{3} = \frac{27}{125}$$

$$\frac{3}{3} \frac{x}{27} + \frac{\cos^8 x}{27} = \frac{2}{125}$$

Cos2 n = 1 - t

Jin² 71 = 3/5

 $\cos^8 x$

 $\tan^2 x = \frac{2}{3}$





$$5(3t^{2}+2(1-t)^{2})=6$$

$$\frac{\sec^{2}n}{a}+\frac{\tan^{2}n}{b}=c$$

$$\tan^{2}n=t$$

$$\sec^{2}n=1+t$$

$$5(3t^{2}+2t^{2}-4t+2)=6$$

$$25t^{2}-20t+4=0$$

$$\left(5t - 2\right)^2 = 0$$

$$\left(5 \pm - 2\right)^2 = 0$$

$$\left(5 \pm 2\right)^2 = 0$$

$$\frac{(3/3)^{4}}{8} + \frac{(3/3)^{4}}{8}$$

$$= \frac{(3/3)^{4}}{8} + \frac{(3/3)^{4}}{8}$$

$$=\frac{2}{54} + \frac{3}{54}$$

$$\frac{54}{54} = \frac{1}{53} = \frac{1}{125}$$

Find
$$tan\frac{\pi}{11} + tan\frac{2\pi}{11} + tan\frac{4\pi}{11} + tan\frac{7\pi}{11} + tan\frac{9\pi}{11} + tan\frac{10\pi}{11}$$

CAST
$$tan(\frac{\pi}{11}) + tan(\frac{2\pi}{11}) + tan(\frac{4\pi}{11}) + tan(\pi - \frac{4\pi}{11}) + tan(\pi - \frac{2\pi}{11}) + tan(\pi - \frac{\pi}{11})$$

$$tan(\frac{\pi}{11}) + tan(\frac{2\pi}{11}) + tan(\frac{4\pi}{11}) - tan(\frac{4$$

$$\tan\left(\frac{\pi}{1}\right) + \tan\left(\frac{\pi}{1}\right) + \tan\left(\frac{\pi}{1}\right) - \tan\left(\frac{\pi}{1}\right) - \tan\left(\frac{\pi}{1}\right) - \tan\left(\frac{\pi}{1}\right)$$

$$\Rightarrow \boxed{0}$$

$$+ \tan(\pi - 0) = -\tan 0$$





Find sin 420° cos 390° + cos(-300°) sin(-330°)



$$\Rightarrow \left(\frac{3}{\sqrt{3}}\right)\left(\frac{3}{\sqrt{3}}\right) - \left(\frac{3}{1}\right)\left(\frac{5}{-1}\right)$$

$$\Rightarrow \frac{3}{4} + \frac{1}{4}$$

$$n\left(2\pi+66^{\circ}\right)$$

=
$$+ \frac{1}{2}$$



The expression $3 \left[\sin^{2} \left(\frac{3\pi}{2} - \alpha \right) + \sin^{4} \left(\frac{3\pi}{2} + \alpha \right) \right] -$

The expression
$$3 \left[\sin^{4} \left(\frac{3\pi}{2} - \alpha \right) + \sin^{4} \left(\frac{3\pi}{2} + \alpha \right) \right] - 2 \left[\sin^{6} \left(\frac{\pi}{2} + \alpha \right) + \sin^{6} \left(5\pi - \alpha \right) \right]$$
 is equal to

$$2\left[\sin^{6}\left(\frac{\pi}{2}+\alpha\right)+\sin^{6}(5\pi-\alpha)\right] \text{ is equal to} \qquad \left(\text{JEE M PYO}\right)$$

$$2\left[\sin^{6}\left(\frac{\pi}{2}+\alpha\right)+\sin^{6}(5\pi-\alpha)\right] \text{ is equal to} \qquad \left(\text{JEE M PYO}\right)$$

$$3\left(\cos^{4}\alpha+\sin^{4}\alpha\right)-2\left(\cos^{6}\alpha+\sin^{6}\alpha\right)$$

$$2\left[\sin^{6}\left(\frac{\pi}{2}+\alpha\right)+\sin^{6}(5\pi-\alpha)\right] \text{ is equal to} \qquad \left(\text{JEE M PYO}\right)$$

 $= 3(1-2x^{2}c^{2})-2(1-3x^{2}c^{2})$



Let $\theta \in \left[0, \frac{\pi}{4}\right]$ and $t_1 = (\tan \theta)^{\tan \theta}$, $t_2 = (\tan \theta)^{\cot \theta}$,

Let
$$\theta \in [0, \frac{1}{4}]$$
 and $t_1 = \frac{(\tan \theta)^{\tan \theta}}{(\tan \theta)^{\cot \theta}}$, $t_2 = \frac{(\tan \theta)^{\cot \theta}}{(\tan \theta)^{\cot \theta}}$
 $t_3 = (\cot \theta)^{\tan \theta}$ and $t_4 = (\cot \theta)^{\cot \theta}$, then

(a)
$$t_1 > t_2 > t_3 > t_4$$
 (b) $t_4 > t_3 > t_1 > t_2 > t_3 > t_4$ (c) $t_3 > t_1 > t_2 > t_4$ (d) $t_2 > t_3 > t_1 > t_4$

$$\theta \in (0, \frac{\pi}{4})$$

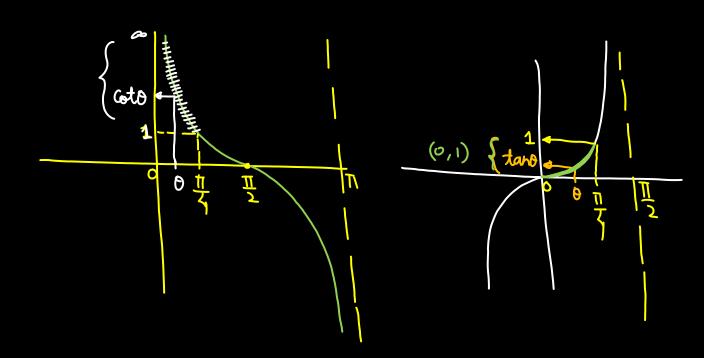
$$\tan \theta \in (0, 1)$$

$$\tan \theta = \frac{1}{2}$$

$$\cot \theta \in (1, \infty)$$

$$\cot \theta = 2$$





Let α, β be such that $\pi < \alpha - \beta < 3\pi$.

Let
$$\underline{\alpha}, \underline{\beta}$$
 be such that $\underline{\pi} < \alpha - \underline{\beta} < 3\pi$.
If $\sin \alpha + \sin \beta = -\frac{21}{65}$ and $\cos \alpha + \cos \beta = -\frac{27}{65}$

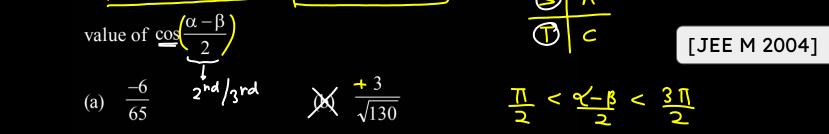
If
$$\sin \alpha + \sin \beta = -\frac{21}{65}$$
 and $\cos \alpha + \cos \beta$



$$e \text{ of } \cos\left(\frac{\alpha - \beta}{2}\right)$$

$$\frac{65}{65} \qquad \frac{\sqrt{130}}{\sqrt{130}} \qquad \frac{2}{2} \qquad \frac{2}{2}$$

$$\frac{6}{65} \qquad \frac{3}{\sqrt{130}} \qquad \frac{3}{\sqrt{130}} \qquad \frac{1}{2} \qquad \frac{1}{2} \qquad \frac{1}{2}$$





$$2 \left(\frac{x}{\sqrt{30}}\right) \cos\left(\frac{x-\beta}{2}\right) = \frac{27}{65}$$

$$2 \cos\left(\frac{x+\beta}{2}\right) \cos\left(\frac{x-\beta}{2}\right) = \frac{-27}{65}$$

$$0-2 \quad \tan\left(\frac{x+\beta}{2}\right) = \frac{7}{9}$$

$$\sin\left(\frac{x+\beta}{2}\right) = \frac{7}{130}$$

$$\left(\cos \left(\frac{\propto -\beta}{2} \right) = \frac{-3}{\sqrt{130}} \right)$$

[JEE M 2022]

$$\frac{1}{\tan \alpha} = 1$$
and $\frac{\pi}{-} < \beta < 1$

If
$$\cot \alpha = 1$$
 and $\sec \beta = -\frac{5}{3}$, where $\frac{\pi < \alpha < \frac{3\pi}{2}}{2}$ and $\frac{\pi}{2} < \beta < \pi$, then the value of $\tan (\alpha + \beta)$ and

the quadrant in which $\alpha + \beta$ lies, respectively are

$$-\frac{1}{7}$$
 and \underline{IV}^{th} quadrant

D.
$$\frac{1}{7}$$
 and I^{st} quadrant

$$tan(x+13) = tanx + tan3$$

$$1 - tanx ton3$$

$$= 1 - \frac{4}{3} = \frac{-1}{3}$$



$$T < x$$

$$T < \beta$$

$$Sec \beta = -\frac{5}{3}$$

$$4 \beta$$

$$T > 3$$

$$T > 3$$

$$T > 3$$

If $a_1, a_2, ..., a_n$ are in A.P. with common difference d then the sum of series $\sin d \left\{ \sec a_1 \sec a_2 + \sec a_2 \sec a_3 + \dots + \sec a_{n-1} \sec a_n \right\}$

$$\sec a_1 - \sec a_n \qquad \qquad \textbf{c.} \quad \cot a_1 - \cot a_n$$

c. $\cot a_1 - \cot a_n$ $\tan a_n - \tan a_1$ $coseca_1 - coseca_n$ В.



$$\frac{\sin(a_2-a_1)}{\cos a_1 \cos a_2}$$

$$\Rightarrow \underline{\lim_{\alpha \to \alpha_1} \cos \alpha_1 - \cos \alpha_2 \cdot \lambda_1 \cos \alpha_1}$$

$$\Rightarrow$$
 tan a_{i} - tan a_{i}

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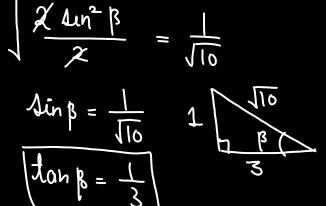
[JEE M 2020]

Let
$$\frac{\sqrt{2}\sin\alpha}{\sqrt{1+\cos2\alpha}} = \frac{1}{7}$$
 and $\sqrt{\frac{1-\cos2\beta}{2}} = \frac{1}{\sqrt{10}}$ where $\alpha, \beta \in \left(0, \frac{\pi}{2}\right)$.

Then tan $(\alpha + 2\beta)$ is equal to

$$\frac{\sqrt{2} \sin \alpha}{\sqrt{2} \cos^2 \alpha} = \frac{1}{4}$$

$$\frac{1}{4} \tan \alpha = \frac{1}{4}$$



 $\alpha, \beta \rightarrow I$



$$tan(\alpha + 2\beta)$$

$$tan(\alpha + 2\beta)$$

$$tan(\alpha + 2\beta)$$

$$tan(\alpha + 2\beta)$$

$$1 - tan(\alpha + 2\beta)$$

$$\frac{1 - \tan \alpha \tan(2\beta)}{1 - \tan^2 \beta} = \frac{2 \tan \beta}{1 - \tan^2 \beta} \\
= \frac{2(\frac{1}{3})}{1 - \frac{1}{4}} = \frac{3}{4}$$



The value of $\cos^2 10^\circ - \cos 10^\circ \cos 50^\circ + \cos^2 50^\circ$ is:

(a)
$$\frac{3}{4} + \cos 20^{\circ}$$
 (b) $3/4$
$$\frac{2 \cos^{2} \Theta}{2} = 1 + \cos 2\Theta$$
 (c) $\frac{3}{2} (1 + \cos 20^{\circ})$ (d) $3/2$
$$2 \cos A \cos B = \cos (A + B) + \cos B$$

$$(c) \frac{1}{2} (1 + \cos 20^{\circ}) \qquad (d) \frac{3}{2} \qquad 2 \cos 4 \cos 8 = \cos (A + B) + \cos (A - B)$$

$$\Rightarrow \frac{1}{2} \left(2 \cos^{2} 10^{\circ} - 2 \cos 10 \cos 50 + 2 \cos^{2} 50 \right)$$

$$\Rightarrow \frac{1}{2} \left((1 + \cos 20) - (\frac{1}{2} + \cos 40) + (1 + \cos 100) \right)$$

$$= \frac{1}{2} \left(\frac{3}{3} + (6320 - (6340 + (63100)) + (14) \right)$$



$$\Rightarrow \frac{1}{3} \left(\frac{3}{2} + 2 \sin 30 \sin 10 + \cos (90 + 10) \right)$$

$$\Rightarrow \frac{1}{3} \left(\frac{3}{2} + 2 \sin 6 - \sin 10 \right)$$

$$\Rightarrow \frac{1}{2} \left(\frac{3}{2} + \text{ sinto} - \text{sinto} \right)$$

$$\Rightarrow \left(\frac{3}{2} \right)$$



The value of $\sin 10^{\circ} \frac{\sin 30^{\circ}}{\sin 50^{\circ}} \frac{\sin 70^{\circ}}{\sin 70^{\circ}}$ is



D.
$$\frac{18}{36}$$

[JEE M 2019]

$$\Rightarrow \frac{1}{2} \left(\frac{4}{4} \times \frac{2}{2} \right)$$



$$Sin(A)$$
 $Sin(60+A)$ $Sin(60-A) = \frac{1}{4}$ $AinsA$
$Cos(60+A)$ $Cos(60-A) = \frac{1}{4}$ $CossA$
$tanA$ $tan(60+A)$ $tan(60-A) = tan(sA)$
$HINT$ $Ain(A+B)$ $Ain(A-B) = Ain^2A - Ain^2B$
= $Cos^2A - Ain^2B$



16sin (20°) sin(40°) sin (80°) is equal to :

[JEE M 2022]





[JEE M 2022]

Q

If $\sin^2(10^\circ) \sin(20^\circ) \sin(40^\circ) \sin(50^\circ) \sin(70^\circ) = \alpha - 1/16 \sin(10^\circ)$, then $16 + \alpha^{-1}$ is equal to_

$$\frac{\sin^2 10}{\sin(20)} \frac{\sin(40)}{\sin(40)} \frac{\sin(50)}{\sin(40)} = \alpha - \frac{1}{16} \frac{\sin(60)}{\sin(60)}$$

$$2 \ln A \ln B = \cos(A - B) - \cos(A + B)$$



2 Lin A Cos B = Sin(A+B) + Sin(A-B)

$$\Rightarrow \frac{1}{16} \left(\frac{\text{Esin10 Co}^{2}20}{2} - \frac{\text{Sin10}}{2} \right)$$

$$\Rightarrow \frac{1}{32} \left(\frac{1}{2} + \text{sin}(10) - \text{sin} 10 \right)$$

$$\Rightarrow \frac{1}{32} \left(\frac{1}{2} - \frac{2}{3} \text{ Lin} | 0 \right)$$

$$\frac{1}{32}\left(\frac{1}{2}\right)$$

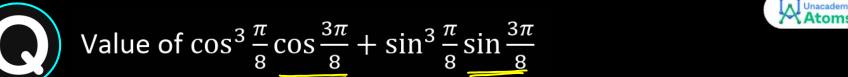
=) ~ - \frac{1}{16} dun 10

 $\propto = \frac{1}{64}$

16+ = 16+64









Value of cos
$$\frac{1}{2\sqrt{2}}$$
 $\frac{1}{2\sqrt{2}}$ $\frac{1}{2\sqrt{2}}$ $\frac{1}{2\sqrt{2}}$ $\frac{1}{2\sqrt{2}}$ $\frac{1}{2\sqrt{2}}$ $\frac{1}{2\sqrt{2}}$ $\frac{1}{2\sqrt{2}}$ $\frac{1}{2\sqrt{2}}$

B.
$$\frac{1}{\sqrt{2}}$$
 \Rightarrow 683 $\frac{\pi}{8}$ Sin $\frac{\pi}{8}$ + Sin $\frac{\pi}{8}$ 68 $\frac{\pi}{8}$

B.
$$\frac{1}{\sqrt{2}}$$

C. $\frac{1}{2}$ \Rightarrow $(68 \frac{\pi}{8} \sin \frac{\pi}{8})$ $(68 \frac{\pi}{8} \sin \frac{\pi}{8})$ [JEE M 2020]

C.
$$\frac{1}{2}$$
 \Rightarrow $\cos \frac{\pi}{8} \sin \frac{\pi}{8} \left(\cos^2 \frac{\pi}{8} + 4m^2 \frac{\pi}{8}\right)$
D. $-\frac{1}{2}$





Let $f: [0,2] \to \mathbb{R}$ be the function defined by

$$f(x) = (3 - \sin(2\pi x))\sin\left(\pi x - \frac{\pi}{4}\right) - \sin\left(3\pi x + \frac{\pi}{4}\right).$$

$$f(\alpha, \beta \in [0, 2])$$
 are such that $\{x \in [0, 2]: f(x) \ge 0\} = [\underline{\alpha, \beta}]$, then the value of $\beta - \alpha$ is _____

$$\left(3 - \sin\left(2\pi\pi\right)\right) \sin\left(\pi x - \frac{\pi}{4}\right) - \sin\left(\frac{3\pi x}{4} + \frac{\pi}{4}\right) \ge 0$$
[JEE]
$$\left(3 - \sin\left(\frac{\pi}{2} + 2\theta\right)\right) \sin\theta - \sin\left(\pi + 3\theta\right)$$

$$\left(3 - \sin\left(\frac{\pi}{2} + 20\right)\right) \sin\theta - \underline{\dim}\left(\pi + 30\right) \ge 0$$

$$\left(3 - \cos 2\theta\right) \underline{\dim}\theta + 3 \sin\theta - 4 \sin^2\theta \ge 0$$

$$\Rightarrow 2\pi x = 2\theta + \frac{\pi}{4}$$

$$\Rightarrow 3\pi x + \frac{\pi}{4} = 3\theta + \pi$$



And
$$(3 - \cos 20 + 3 - 4 \sin^2 \theta) \ge 0$$

Sin θ $(6 - (1 - 2 \sin^2 \theta) - 4 \sin^2 \theta) \ge 0$

Sin θ $(5 - 2 \sin^2 \theta) \ge 0$

And $\theta \in [0,1]$

The sin $\theta \in [0,1]$

The sin





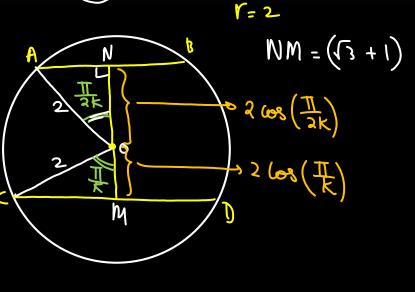
Two parallel chords of a circle of radius 2 are at a distance



 $\sqrt{3}$ +1 apart. If the chords subtend at the center, angles of

$$\left(\frac{\pi}{k}\right)$$

and $\frac{2k}{k}$ where k > 0, then the value of [k] is



[JEE Adv. 2010]



$$2 \omega s \left(\frac{\pi}{2k}\right) + 2 \cos \left(\frac{\pi}{k}\right) = \sqrt{3} + 1$$

$$\left(\frac{\pi}{2k}\right) = 0 \implies \left(\frac{\pi}{k}\right) = 20$$

$$2 (680 + 2 (6820 = \sqrt{3} + 1))$$

$$2(680 + 2(6820 = \sqrt{3} + 1)$$

$$2 \cos \theta + 2 (2 \cos^2 \theta - 1) = \sqrt{3} + 1$$

$$\frac{4 \cos^2 \theta + 2 \cos \theta - (3+13) = 0}{\cos^2 \theta + 2 \cos \theta - (3+13) = 0}$$





$$\cos \theta = \frac{-1 \pm \sqrt{13 + 4\sqrt{3}}}{4}$$

$$= (2\sqrt{3})^{2} + (1)^{2} + 2(2\sqrt{3})(1)$$

$$= -1 \pm (213 + 1)$$

73--

[JEE Adv 2022]

Let α and β be real numbers such that $-\frac{\pi}{4} < \beta < 0 < \alpha < \frac{\pi}{4}$. If $\sin(\alpha + \beta) = \frac{1}{3}$ $\cos(\alpha - \beta) = \frac{2}{3}$, then the greatest integer less than or equal to

$$\left(\frac{\sin\alpha}{\cos\beta} + \frac{\cos\beta}{\sin\alpha} + \frac{\cos\alpha}{\sin\beta} + \frac{\sin\beta}{\cos\alpha}\right) \Rightarrow \frac{16}{9}$$

is

 $\frac{\cos(\alpha-\beta)}{\sin\beta \cos\beta} + \frac{\cos(\alpha-\beta)}{\sin\alpha \cos\alpha}$



$$\Rightarrow \frac{4}{3} \left(\frac{1}{\text{Aun}_2 \beta} + \frac{1}{\text{Aun}_2 \gamma} \right)$$

$$\Rightarrow \frac{2x4}{3} \left(\frac{\sin 2x + \sin 2x}{2 \sin 2x + \sin 2x} \right)$$

$$\Rightarrow \frac{8}{3} \left(\frac{2 \left(\frac{1}{3} \right) \left(\frac{2}{3} \right)}{\left(\frac{2}{3} \right) - \left(\frac{2}{3} \right) - \left(\frac{2}{3} \right)} \right)$$

$$\Rightarrow \frac{32}{27} \left(\frac{(3 \log^2(\alpha - 2\beta) - (03(2\alpha + 2\beta)))}{(3 \log^2(\alpha - \beta) - 1) - (1 - 2 \sin^2(\alpha + \beta))} \right)$$



$$\Rightarrow \frac{3^2}{27} \left(\frac{2\left(\frac{2}{3}\right)^2 - 1 - \left(1 - 2\left(\frac{1}{3}\right)^2\right)}{\left(2\left(\frac{2}{3}\right)^2 - 1\right) - \left(1 - 2\left(\frac{1}{3}\right)^2\right)} \right)$$

$$\Rightarrow \frac{32}{27} \left(\frac{1}{\left(-\frac{1}{q} \right) - \left(\frac{7}{q} \right)} \right)$$

$$\frac{32}{27} \times \frac{9}{-8} = \frac{16}{9}$$



The value of $2\sin(12^\circ) - \sin(72^\circ)$ is:

4.
$$\frac{\sqrt{5(1-\sqrt{3})}}{4}$$
 B. $\frac{1-\sqrt{5}}{8}$

c.
$$\frac{\sqrt{3}(1-\sqrt{5})}{2}$$
 $\frac{\sqrt{3}(1-\sqrt{5})}{4}$

Am 12 + din 12 - den 72

[JEE M 2022]



$$\Rightarrow -\chi \times \left(\frac{\sqrt{3}}{2}\right) \left(\frac{\sqrt{5}-1}{4}\right)$$



$\alpha = \sin 36^{\circ}$ is a root of which of the following equation

A.
$$10x^4 - 10x^2 - 5 = 0$$

8.
$$16x^4 + 20x^2 - 5 = 0$$

C.
$$16x^4 - 20x^2 + 5 = 0$$

D.
$$16x^4 - 10x^2 + 5 = 0$$

$$|6\alpha|^2 = 10 - 2\sqrt{5}$$

$$(\sqrt{5}) = (5 - 8)$$

[JEE M 2022]





Prove that
$$\cos \frac{\pi}{15} \cos \frac{2\pi}{15} \cos \frac{3\pi}{15} \cos \frac{4\pi}{15} \cos \frac{5\pi}{15} \cos \frac{6\pi}{15} \cos \frac{7\pi}{15} = \frac{1}{128}$$

$$- \left(\cos \frac{\pi}{15} \cos \frac{2\pi}{15} \cos \frac{4\pi}{15} \cos \frac{5\pi}{15} \cos \frac{6\pi}{15} \cos \frac{7\pi}{15}\right) \cos \frac{\pi}{15}$$

$$\frac{4 \ln \left(2^{4} \cdot \frac{11}{15}\right)}{2^{4} 4 \ln \frac{11}{15}} \left[\frac{4 \ln \left(2^{2} \cdot \frac{3\pi}{15}\right)}{2^{2} 4 \ln \left(\frac{3\pi}{15}\right)}\right] \left[\frac{1}{2}\right]$$

$$-\left[\begin{array}{c}2^{7} \operatorname{Aun} \frac{11}{15}\\15\end{array}\right]\left(\begin{array}{c}2^{2} \operatorname{Aun} \left(\frac{311}{15}\right)\\2^{4} \operatorname{Aun} \frac{11}{15}\end{array}\right]\left(\begin{array}{c}2^{2} \operatorname{Ain} \left(\frac{1211}{15}\right)\\2^{2} \operatorname{Ain} \left(\frac{311}{15}\right)\end{array}\right)\left(\begin{array}{c}2\\2\end{array}\right)$$

$$\left|\frac{t^2}{2l}\right| \approx 1$$

$$\int_{-\infty}^{\infty} \left|\frac{t^2}{2l}\right| \approx 1$$



$$\frac{Jn(\Pi + \overline{IS})}{2^4 Jn(\overline{IS})} \frac{Jn(\Pi - 3\overline{II})}{2^2 Jn(\frac{3\overline{II}}{IS})}$$

$$\frac{Jn(\Pi + \overline{IS})}{2^4 Jn(\overline{IS})} \frac{Jn(\frac{3\overline{II}}{IS})}{2^4 Jn(\overline{IS})}$$

$$\frac{Jn(\Pi + \overline{IS})}{2^4 Jn(\overline{IS})} \frac{Jn(\frac{3\overline{II}}{IS})}{2^2 Jn(\frac{3\overline{II}}{IS})}$$

$$\frac{Jn(\Pi + \overline{IS})}{2^4 Jn(\overline{IS})} \frac{Jn(\frac{3\overline{II}}{IS})}{2^2 Jn(\frac{3\overline{II}}{IS})}$$

Prove that $\sin \frac{\pi}{14} \sin \frac{3\pi}{14} \sin \frac{5\pi}{14} \sin \frac{7\pi}{14} = \frac{1}{8}$ $\Rightarrow \cos\left(\frac{\pi}{2} - \frac{\pi}{14}\right) \cos\left(\frac{\pi}{2} - \frac{3\pi}{14}\right) \cos\left(\frac{\pi}{2} - \frac{5\pi}{14}\right) \times 1$

$$\cos\left(\frac{1}{2} - \frac{14}{14}\right)$$

$$\cos\left(\frac{6\pi}{14}\right)$$

$$\Rightarrow$$
 Cos $\left(\frac{6\pi}{14}\right)$ Cos $\left(\frac{4\pi}{14}\right)$ Cos $\left(\frac{2\pi}{14}\right)$

$$\left(\frac{1}{4}\right)$$
 so $\left(\frac{1}{4}\right)$ so $\left(\frac{$

$$\Rightarrow (os(\frac{\pi}{7}) cos(\frac{2\pi}{7}) cos(\frac{3\pi}{7})$$

$$\frac{1}{14}$$

$$3\left(\frac{2\Pi}{14}\right)$$

$$Sin\theta = GS\left(\frac{\pi}{2} - \theta\right)$$

(12) Earl

 $= 68 \left(T - 4T \right)$

 $=-\left(\cos\left(\frac{\pi}{4}\right)\right)$



$$\Rightarrow - \frac{\sin\left(2^3 \cdot \frac{\pi}{4}\right)}{2^3 \sin\left(\frac{\pi}{4}\right)}$$

$$\Rightarrow \frac{1}{8}$$

$$Sin\left(\pi + \frac{\pi}{4}\right)$$

$$= -8in\left(\frac{\pi}{4}\right)$$





Prove that
$$\sin \frac{\pi}{5} \sin \frac{2\pi}{5} \sin \frac{3\pi}{5} \sin \frac{4\pi}{5} = \frac{5}{16}$$

H.W. Cos

$$2\sin\left(\frac{\pi}{22}\right)\sin\left(\frac{3\pi}{22}\right)\sin\left(\frac{5\pi}{22}\right)\sin\left(\frac{7\pi}{22}\right)\sin\left(\frac{9\pi}{22}\right)$$

is equal to
$$2 \cos \left(\frac{\pi}{2} - \frac{\pi}{22}\right) \cos \left(\frac{\pi}{2} - \frac{3\pi}{22}\right) \cos \left(\frac{\pi}{2} - \frac{5\pi}{22}\right) \cos \left(\frac{\pi}{2} - \frac{7\pi}{22}\right) \cos \left(\frac{\pi}{2} - \frac{\pi}{22}\right) \cos \left(\frac{\pi}{2} - \frac{\pi}{22}\right$$

A.
$$\frac{3}{16}$$

c.
$$\frac{1}{30}$$

c.
$$\frac{1}{32}$$
 D. $\frac{9}{32}$

$$2 \left(\frac{|0\Pi|}{22} \right) \left(\frac{8\Pi}{22} \right) \left(\frac{6\Pi}{22} \right) \left(\frac{6\Pi}{22} \right) \left(\frac{4\Pi}{22} \right) \left(\frac{2\Pi}{22} \right) = \left(\frac{6\Pi}{11} \right)$$

$$= \left(\frac{6\Pi}{11} \right)$$

$$\Rightarrow 2 \cos \left(\frac{2\pi}{1}\right) \cos \left(\frac{2\pi}{1}\right) \cos \left(\frac{2\pi}{1}\right) \cos \left(\frac{2\pi}{1}\right) \cos \left(\frac{2\pi}{1}\right)$$

$$\Rightarrow 2 \left(\cos \frac{\pi}{1}\right) \cos \left(\frac{2\pi}{1}\right) \cos \left(\frac{2\pi}{1}\right) \left(-\cos \left(\frac{2\pi}{1}\right)\right) \cos \left(\frac{2\pi}{1}\right)$$

$$\Rightarrow -2 \left(\frac{Ain(2^3 \frac{\pi}{1})}{2^3 Ain(\frac{\pi}{1})}\right) \left(\frac{Ain(2^2 \frac{3\pi}{1})}{2^2 Ain(\frac{3\pi}{1})}\right) = din(\frac{12\pi}{11})$$

$$\Rightarrow -2 \left(\frac{\text{Ain}(2^3 \frac{11}{11})}{2^3 \text{Ain}(\frac{11}{11})} \right) \left(\frac{\text{Aun}(2^2 \frac{311}{11})}{2^2 \text{Aun}(\frac{311}{11})} \right) = \frac{\text{Aun}(\frac{1211}{11})}{2^3 \text{Ain}(\frac{311}{11})} \left(\frac{\text{Aun}(\frac{311}{11})}{2^2 \text{Ain}(\frac{311}{11})} \right) = -\frac{\text{Aun}(\frac{11}{11})}{2^3 \text{Ain}(\frac{311}{11})}$$



[JEE M 2019]

The value of

$$\cos \frac{\pi}{2^2} \cos \frac{\pi}{2^3} \dots \cos \frac{\pi}{2^{10}} \sin \frac{\pi}{2^{10}}$$

$$\frac{1}{512}$$
 COS $\frac{1}{2^3}$... COS $\frac{1}{2^{10}}$ SIII $\frac{1}{2^{10}}$ C. $\frac{1}{256}$

A.
$$\frac{1}{512}$$
 C. $\frac{1}{256}$ B. $\frac{1}{1024}$ D. $\frac{1}{2}$

$$\cos\left(\frac{\pi}{2^{10}}\right)$$
 $\cos\left(\frac{\pi}{2^{9}}\right)$. $\cos\left(\frac{\pi}{2^{3}}\right)$ $\cos\left(\frac{\pi}{2^{2}}\right)$. $\sin\left(\frac{\pi}{2^{10}}\right)$

$$\Rightarrow \frac{\sin\left(2^{9} \frac{\pi}{2^{10}}\right)}{2^{9} \sin\left(\frac{\pi}{2^{10}}\right)} + \sin\left(\frac{\pi}{2^{10}}\right) \Rightarrow \frac{1}{512}$$





Find the sum of series $\frac{\cos \frac{\pi}{11} + \cos \frac{3\pi}{11} + \cos \frac{5\pi}{11} + \cos \frac{7\pi}{11} + \cos \frac{9\pi}{11}$.

$$\begin{array}{ccc}
\text{O SUM} \\
\text{O A P}
\end{array}$$

$$\begin{array}{cccc}
\alpha = \frac{\pi}{11} & \beta = \frac{2\pi}{11} & \beta = \frac{\pi}{11} \\
\end{array}$$

$$M = S$$

$$M = S$$

$$m = 5$$

$$Ain (nB)$$

| $\frac{4m(\frac{B}{2})}{4m(\frac{B}{2})} \cos \left(\alpha + \frac{(n-1)}{2} \right)$ |
|---|
| $\frac{\operatorname{Im}\left(\frac{5}{11}\right)}{\operatorname{Ain}\left(\frac{11}{11}\right)} \cos\left(\frac{11}{11} + 4\frac{11}{11}\right)$ |



$$= \frac{2 \sin \left(\frac{5\pi}{11}\right) \cos \left(\frac{5\pi}{11}\right)}{2 \sin \left(\frac{\pi}{11}\right)}$$

$$\Rightarrow \frac{\sin\left(\frac{10\pi}{11}\right)}{2 \sin\left(\frac{10\pi}{11}\right)} = \frac{\sin\left(\frac{\pi}{11}\right)}{2 \sin\left(\frac{\pi}{11}\right)} = \frac{1}{2}$$

 $su(\frac{3ti}{7})$

= din(11-41)
= + din 41

is equal to:

du I

D.

The value of $\cos\left(\frac{2\pi}{7}\right) + \cos\left(\frac{4\pi}{7}\right) + \cos\left(\frac{6\pi}{7}\right)$

Sum

[JEE M 2022]

n = 3



$$\frac{2 \operatorname{din} \left(\frac{47}{7}\right) \operatorname{cos} \left(\frac{47}{7}\right)}{2 \operatorname{din} \left(\frac{7}{7}\right)}$$

$$\frac{\operatorname{din} \left(\frac{7}{7}\right)}{2 \operatorname{din} \left(\frac{7}{7}\right)}$$

$$= \frac{1 \operatorname{din} \left(\frac{7}{7}\right)}{2 \operatorname{din} \left(\frac{7}{7}\right)}$$



The value of $\sum_{k=1}^{15} \frac{(15)}{\sin\left(\frac{\pi}{4} + \frac{(k-1)\pi}{6}\right) \sin\left(\frac{\pi}{4} + \frac{k\pi}{6}\right)}$ is equal to



[JEE Adv. 2016]

(a)
$$3-\sqrt{3}$$
 (b) $2(3-\sqrt{3})$ (c) $2(\sqrt{3}-1)$ (d) $2(2-\sqrt{3})$ (e) $2(\sqrt{3}-1)$ (ii) $2(\sqrt{3}-1)$ (iii) $2(\sqrt{3}-1)$ (iii)



$$\frac{\sin(\beta-A)}{\sinh \sin A} = \frac{\sin \beta \cos A - \cos \beta \sin A}{\sin A \sin \beta} = \cot A - \cot \beta$$

$$2 \underbrace{\begin{cases} 3}{k=1} \cot \left(\frac{\pi}{4} + \frac{(k-1)\pi}{6}\right) - \cot \left(\frac{\pi}{4} + \frac{k\pi}{6}\right)}_{\text{K=1}} \cot \left(\frac{\pi}{4} + \frac{\pi}{6}\right) - \cot \left(\frac{\pi}{4} + \frac{\pi}{6}\right) + \cot \left(\frac{3\pi + 26\pi}{12}\right)$$

$$\cot \left(\frac{\pi}{4} + \frac{\pi}{6}\right) - \cot \left(\frac{\pi}{4} + \frac{2\pi}{6}\right) + \cot \left(\frac{2\pi + 2\pi}{12}\right)$$

$$\cot \left(\frac{\pi}{4} + \frac{\pi}{6}\right) - \cot \left(\frac{\pi}{4} + \frac{3\pi}{6}\right) + \cot \left(\frac{2\pi + 2\pi}{12}\right)$$

$$\cot \left(\frac{\pi}{4} + \frac{\pi}{6}\right) - \cot \left(\frac{\pi}{4} + \frac{3\pi}{6}\right) + \cot \left(\frac{2\pi}{4} + \frac{3\pi}{12}\right)$$

$$5 = 2\left(1 - \cot \frac{3\pi}{12}\right)$$

$$5 = 2\left(1 - \cot \frac{3\pi}{12}\right)$$



tan(45-30)

$$S = 2(1 - \cot 75^{\circ})$$

$$= 2(1 - (2 - \sqrt{3}))$$

$$= 2(\sqrt{3} - 1)$$

$$= 2(\sqrt{3} - 1)$$

$$= 2(\sqrt{3} - 1)$$

$$= 2(\sqrt{3} - 1)$$



[JEE M 2022]

Then

A.
$$S = \left\{ \frac{\pi}{12} \right\}$$

$$\lfloor 12 \rfloor$$

$$\sum \alpha_{-}$$

$$\sum \theta =$$

$$\sum \theta =$$

$$\theta = \frac{\pi}{2}$$

Let $S = \left\{ \theta \in \left(0, \frac{\pi}{2}\right) : \sum_{m=1}^{9} \sec\left(\theta + \left(m-1\right)\frac{\pi}{6}\right) \sec\left(\theta + \frac{m\pi}{6}\right) = -\frac{8}{\sqrt{3}} \right\}$

 $S = \left\{ \frac{2\pi}{3} \right\}$

$$\sum_{\Omega = \Gamma} \theta = \frac{\pi}{2}$$

$$\sum_{\theta \in S} \theta = \frac{\pi}{2}$$

$$\sum_{\theta \in S} \theta = \frac{3\pi}{4}$$

$$\sum_{\theta \in S} \theta = \frac{3\pi}{4}$$

$$\leq \theta = \frac{\pi}{6} + \frac{\pi}{3} = \frac{\pi}{2}$$

CosA CosB

Link Cost - Cost Linh

CosA CosB

tan B - tank

$$\frac{2}{\cos\left(\theta+(m-1)\frac{\pi}{6}\right)-\left(0+(m-1)\frac{\pi}{6}\right)}$$

$$\frac{\cos\left(\theta+(m-1)\frac{\pi}{6}\right)}{A} \cos\left(\theta+\frac{m\pi}{6}\right)$$

$$\frac{\pi}{6}$$

$$\frac{\pi$$

$$2) = \frac{9}{m=1} \tan \left(\theta + \frac{m\pi}{6}\right) - \tan \left(\theta + \frac{m-1}{6}\right)$$

$$2 = \frac{9}{m=1} \tan \left(\theta + \frac{m\pi}{6}\right) - \tan \left(\theta + \frac{m-1}{6}\right)$$

$$\frac{9}{m=1} \tan \left(\theta + \frac{m\pi}{6}\right) - \tan \left(\theta + \frac{m-1}{6}\right)$$

$$\tan \left(\theta + \frac{m\pi}{6}\right) - \tan \left(\theta\right)$$

$$\frac{9}{m=1} \tan \left(\theta + \frac{m\pi}{6}\right) - \tan \left(\theta + \frac{m-1}{6}\right)$$

$$\tan \left(\theta + \frac{\pi}{6}\right) - \tan \left(\theta\right)$$

$$\frac{1}{2} = \tan \left(\theta + \frac{m\pi}{6}\right) - \tan \left(\theta + \frac{m-1}{6}\right)$$

$$\frac{9}{4} \quad \tan \left(\theta + \frac{m\pi}{6} \right) - \tan \left(\theta + \frac{m-1}{6} \right)$$

$$B - A = \frac{\pi}{6}$$

$$A \qquad B$$

$$A \qquad B$$

$$A \qquad B \qquad A \qquad B$$



$$S = 2 \left(\tan \left(0 + \frac{3\pi}{2} \right) - \tan \theta \right)$$

$$\Rightarrow 2\left(+\cot\theta + \tan\theta\right) = \frac{1}{\sqrt{3}}$$

$$\frac{1 \times 5}{1 \times 5} = \frac{1}{3}$$

$$\frac{1 \times 5}{1 \times 5} = \frac{1}{3}$$

$$30 = \frac{3}{\sqrt{3}}$$

$$Q\theta = \frac{\pi}{3}, \pi - \frac{\pi}{3}$$

$$\theta = \frac{\pi}{3}, \frac{\pi}{3}$$

Illustratio
$$y = \sin^{2}\left(\frac{15\pi}{8} - 4x\right) - \sin^{2}\left(\frac{17\pi}{8} - 4x\right). \text{ Find range of } y.$$

$$y = \sin^{2}\left(\frac{15\pi}{8} - 4x\right) - \sin^{2}\left(\frac{17\pi}{8} - 4x\right). \text{ Find range of y.}$$

$$y = \text{Aun}\left(\left(\frac{15\pi}{8} - 4x\right) + \left(\frac{17\pi}{8} - 4x\right)\right). \text{ Aun}\left(\left(\frac{15\pi}{8} - 4x\right) - \left(\frac{17\pi}{8} - 4x\right)\right)$$

$$y = \sin^{2}\left(\frac{15\pi}{8} - 4x\right) - \sin^{2}\left(\frac{17\pi}{8} - 4x\right). \text{ Find range of } y.$$

$$y = -4\pi\left(\frac{15\pi}{8} - 4x\right) + \left(\frac{17\pi}{8} - 4x\right). \text{ dun}\left(\frac{15\pi}{8} - 4x\right) - \left(\frac{17\pi}{8} - 4x\right)$$

$$y = -4\pi\left(\frac{17\pi}{8} - 4x\right) + \left(\frac{17\pi}{8} - 4x\right). \text{ dun}\left(\frac{15\pi}{8} - 4x\right) - \left(\frac{17\pi}{8} - 4x\right)$$

$$y = -4\pi\left(\frac{15\pi}{8} - 4x\right) + \left(\frac{17\pi}{8} - 4x\right). \text{ dun}\left(\frac{15\pi}{8} - 4x\right) - \left(\frac{17\pi}{8} - 4x\right)$$

$$y = -4\pi\left(\frac{17\pi}{8} - 4x\right) + \left(\frac{17\pi}{8} - 4x\right). \text{ dun}\left(\frac{15\pi}{8} - 4x\right) - \left(\frac{17\pi}{8} - 4x\right)$$

$$y = -4\pi\left(\frac{17\pi}{8} - 4x\right) + \left(\frac{17\pi}{8} - 4x\right). \text{ dun}\left(\frac{15\pi}{8} - 4x\right) - \left(\frac{17\pi}{8} - 4x\right)$$

$$y = -4\pi\left(\frac{17\pi}{8} - 4x\right) + \left(\frac{17\pi}{8} - 4x\right). \text{ dun}\left(\frac{15\pi}{8} - 4x\right) - \left(\frac{17\pi}{8} - 4x\right)$$

$$= -7\pi\sin(8x) + 4\pi\pi \left(\frac{17\pi}{8} - 4x\right). \text{ dun}\left(\frac{15\pi}{8} - 4x\right)$$

$$= -7\pi\sin(8x) + 4\pi\pi \left(\frac{17\pi}{8} - 4x\right). \text{ dun}\left(\frac{17\pi}{8} - 4x\right)$$

$$y = \sin^{2}\left(\frac{15\pi}{8} - 4x\right) - \sin^{2}\left(\frac{17\pi}{8} - 4x\right). \text{ Find range of y.}$$

$$y = -4\pi\left(\frac{15\pi}{8} - 4\pi\right) + \left(\frac{17\pi}{8} - 4\pi\right). \text{ Aun}\left(\frac{15\pi}{8} - 4\pi\right) - \left(\frac{17\pi}{8} - 4\pi\right)$$

$$y = -4\pi\left(\frac{4\pi}{8} - 4\pi\right) + \left(\frac{17\pi}{8} - 4\pi\right). \text{ Aun}\left(\frac{15\pi}{8} - 4\pi\right) - \left(\frac{17\pi}{8} - 4\pi\right)$$

$$y = \operatorname{Jan}\left(\frac{8\pi}{8} - 4\pi\right) + \left(\frac{17\pi}{8} - 4\pi\right). \operatorname{Jan}\left(\left(\frac{15\pi}{8} - 4\pi\right) - \left(\frac{17\pi}{8} - 4\pi\right)\right)$$

din 82 (-1, 1)





If the equation $\cos^4 \theta + \sin^4 \theta + \lambda = 0$ has real

If the equation
$$\cos^4\theta + \sin^4\theta + \lambda = 0$$
 has real solutions for θ , then $\widehat{\lambda}$ lies in interval
$$\lambda = -\left(\lambda \ln^4\theta + \cos^4\theta\right)$$
[JEE M 2020]
$$\lambda = -\left(1 - \frac{4\lambda \ln^2\theta}{4\lambda \ln^2\theta}\right)$$

$$(C) \left(-\frac{1}{2}, -\frac{1}{4}\right]$$

$$(D) \left(-\frac{5}{4}, -1\right)$$

$$0 \leq \sin^{2} 2\theta \leq 1$$

$$\lambda = -\left(\frac{1 - 4 \sin^2 \theta + \cos^4 \theta}{1 - 4 \sin^2 \theta \cos^2 \theta}\right)$$

$$\lambda = -\left(1 - \frac{4 \sin^2 \theta \cos^2 \theta}{2}\right)$$

$$\lambda = \frac{4 \sin^2 2\theta}{2} - 1$$

$$=\frac{4\pi n^2 2\theta}{2}$$

$$=\frac{4\pi^2 2\theta}{2}$$

$$=\frac{2}{2}$$

$$=\frac{2}{2}$$

$$=\frac{2}{2}$$

$$\frac{1}{2} = \frac{4 \ln^2 20}{2}$$

$$\frac{1}{2} = \frac{0}{2} - 1 = -1$$

$$\frac{1}{2} = \frac{1}{2} - 1 = -\frac{1}{2}$$





The maximum value of the expression
$$1 \times 2$$
.

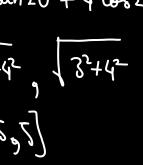
$$\frac{1 \times 2}{\sin^2 \theta + 3 \sin \theta \cos \theta + 5 \cos^2 \theta}$$
 is

$$2 \left(\sin^2\theta + 3\sin\theta\cos\theta + 5\cos^2\theta\right)^{-2}$$

$$1 - \frac{\cos 2\theta + 3 \sin 2\theta + 5(1 + \cos 2\theta)}{\cos 2\theta + \cos 2\theta + \cos 2\theta}$$

$$\Rightarrow \frac{2}{3 \sin 2\theta + \ln 2\theta}$$

$$= \frac{2}{[-5,5]+6} = \frac{2}{-5+6} = 2$$







(1)

Conditional Identities





A+B+C=T



(2)
$$\cos 2A + \cos 2B + \cos 2C = -1 - 4 \cos A \cos B \cos C$$

(3)
$$\sin A + \sin B + \sin C = 4\cos\frac{A}{2}\cos\frac{B}{2}\cos\frac{C}{2}$$

(4)
$$\cos A + \cos B + \cos C = 1 + 4 \sin \frac{A}{2} \sin \frac{B}{2} \sin \frac{C}{2}$$

(5)
$$\tan A + \tan B + \tan C = \tan A \tan B \tan C$$

(6)
$$\tan \frac{A}{2} \tan \frac{B}{2} + \tan \frac{C}{2} \tan \frac{B}{2} + \tan \frac{C}{2} \tan \frac{A}{2} = 1$$







$$\Rightarrow 2 \frac{\text{Lin}(A+B)}{\text{Cos}(A-B)} + 2 \frac{\text{Lin}(Cos)}{\text{Cos}(A-B)} + 2 \frac{\text{Lin}(Cos)}{\text{Cos}(A-B)}$$

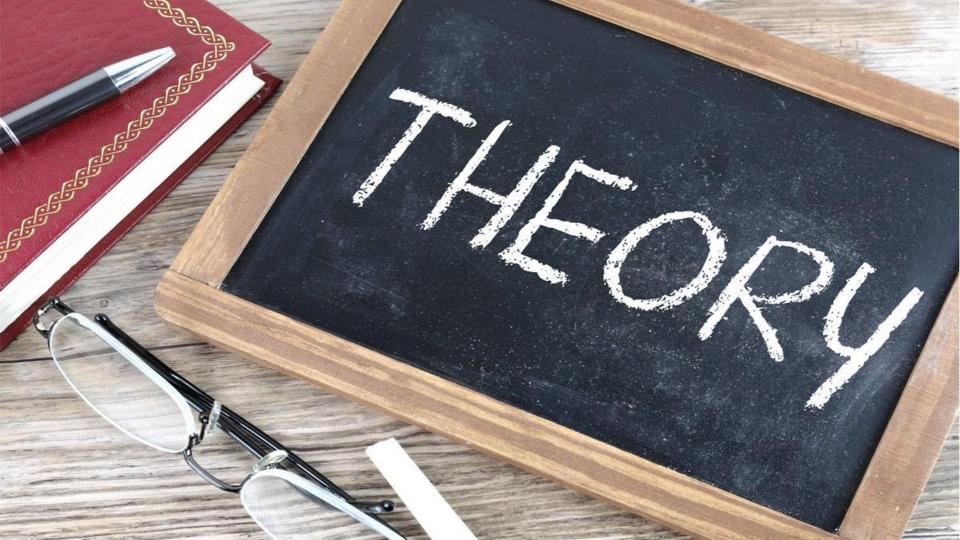
$$uh \in \omega_3(A-1) + 2\pi uh \in \omega_3C$$

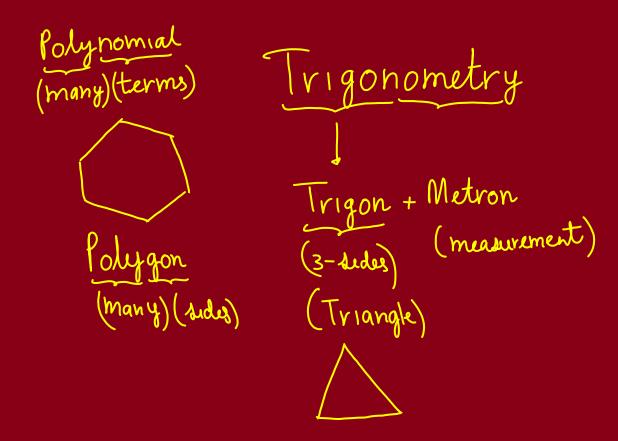
$$\Rightarrow 2 \sin \left((2) \cos \left(A - B \right) + (3) \cos \left(C \right) \right)$$

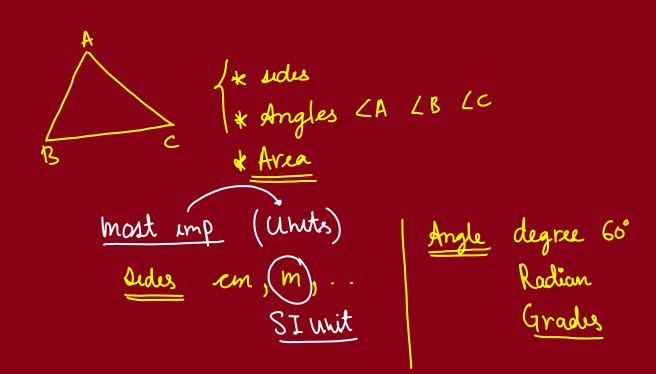
$$\Rightarrow 2 \sin \left((2) \cos \left(A - B \right) + (3) \cos \left(C \right) \right)$$

A+B= T- -Sin (A+B) = Jun (T-C) = June









30° = 30×1° m = 30 x 60' -, cm = [800] System of Unit -, dm 1m = 100cm (SI)(ircular English unitial System (grades) (degree) Radian

$$180^{\circ} = \pi \text{ rad}$$

$$\frac{180^{\circ}}{6} = \frac{\pi}{6} \text{ rad}$$

$$30^{\circ} = \frac{\pi}{6} \text{ rad}$$

$$60^{\circ} = \frac{\pi}{3} \text{ rad}$$

$$90^{\circ} = \frac{\pi}{2} \text{ rad}$$

$$30° = 80 \times \frac{\pi}{280} = \frac{\pi}{6}$$

$$120_{\circ} = 120 \times \frac{180}{4} = \frac{6}{24}$$

$$|50 = 5 \times 30|$$
 $|300 = |0 \times 30|$
= $|01|$
= $|01|$

Remember

$$180^{\circ} = \pi \text{ rad}$$

$$90^{\circ} = \frac{\pi}{2} \text{ rad}$$

$$45^{\circ} = \frac{\pi}{4} \text{ rad}$$

$$60^{\circ} = \frac{\pi}{3}$$

$$36^{\circ} = \frac{\pi}{6}$$

Arc Length

Area of Sector 1-

$$A = \frac{1}{2} \theta r^{2}$$

$$\# \left(= r\theta \right)$$

$$\# \left(\frac{1}{2} \theta r^{2} \right)$$

$$A = \frac{1}{2} \theta r^{2}$$

$$3 \text{ an } \# l = V0$$

$$= 3 \times \frac{11}{6}$$

$$= \frac{11}{2} = \frac{314}{2} = 1.57 \text{ cm}$$

$$\# A = \frac{1}{2} \theta r^{2}$$

$$= \frac{1}{2} \left(\frac{\pi}{8} \right) (8)(3) = \frac{3\pi}{4} = \frac{3(314)}{4} = \boxed{\text{cm}^{2}}$$

$$suc^2 \theta + cos^2 \theta = 1$$
$suc^2 \theta - tan^2 \theta = 1$
$cose^2 \theta - (ot^2 \theta = 1)$

Complimentry Angle Identity

$$Jin (90-0) = Coso$$

$$Jun\left(\frac{\pi}{2} - \theta\right) = CeS\theta$$

$$\cos\left(\frac{1}{2} - \theta\right) = \sin\theta$$

$$\tan\left(\frac{11}{2}-0\right)=\cot\theta$$

$$\cot\left(\frac{\pi}{2}-\theta\right) = \tanh\theta$$

$$\left(\cot\left(\frac{\pi}{2}-\theta\right) = \det\theta$$

$$4e(\left(\frac{\pi}{2}-\theta\right)=\cos(\theta)$$

11th trigo
$$(a+b)^{3} = a^{3} + b^{3} + 3ab(a+b)$$
#1 $\int_{0}^{4} \frac{1}{a^{2}} + \frac{1}{a^$

#2
$$\sin^6 \theta + (\cos^6 \theta = 1 - 3 \sin^2 \theta \cos^2 \theta)$$

$$\frac{\#1}{\pi} \left(4u^2 \theta^2 + (6s^2 \theta^2) - 2ab \right)$$
= $\left(4u^2 \theta^2 + (6s^2 \theta^2) - 2ab \right) - 2ab = (0 + 6s^2 \theta^2)$

$$= 1 - 2 \sin^2\theta \cos^2\theta$$

$$= sun^60 + cos^60$$

$$= \left(\lambda \ln^2 \theta \right)^3 + \left(\cos^2 \theta \right)^3$$

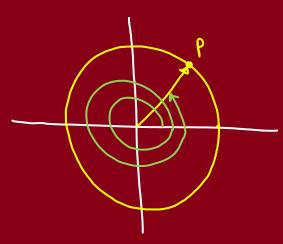
$$= \left(\lambda \ln^2 \theta + (\cos^2 \theta) \right) \left(\frac{\lambda \ln^4 \theta + (\cos^4 \theta)}{2} - \lambda \ln^2 \theta \cos^2 \theta \right)$$

$$= (4in^{2}\theta + (6s^{2}\theta))(4in^{4}\theta + (6s^{4}\theta - 4in^{2}\theta (6s^{2}\theta))$$

$$= (4)(4-24in^{2}\theta (6s^{2}\theta - 4in^{2}\theta (6s^{2}\theta))$$

CAST rule.

Rad=r



Allied Angles

$$din\theta = Ain(2\pi + \theta) = Sin(4\pi + \theta)$$

tano
wto
wto
wto

Sin 120° Sin 180°

$$\frac{CAST}{ASTC}$$

$$\frac{Ede 2}{Eule 2}$$

$$\frac{Eule 2}{Eun(+)}$$

$$\frac{Eule 2}{Eule 2}$$

$$\frac{Eule 2}{Eule 3}$$

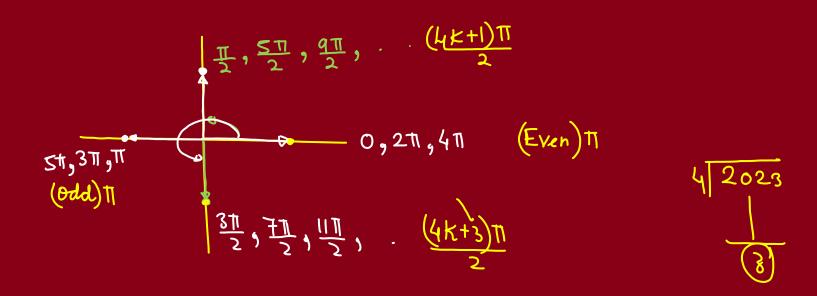
$$\frac{Eule 2}{Eule 4}$$

$$\frac{Eule 2}{Eule 2}$$

$$\frac{Eule 2}{Eule 3}$$

$$\frac{Eule 2}{Eule 4}$$

$$\frac{Eule 2}$$



ACW(+) CW(-)

$$\sin\left(\frac{3\pi}{2} - \theta\right) = -\cos\theta$$
$\tan\left(2\pi - \theta\right) = -\tan\theta$

Sec
$$\left(\frac{11\pi}{2} + 0\right) = +\cos 2\theta$$

$\frac{2023\pi}{2} + 0 = -\cos 0$

$\cot \left(2021\pi + 20\right) = +\cot (20)$

Negative Angles

$$\int_{0}^{\infty} \sin(-\theta) = -\sin\theta$$

$$\int_{0}^{\infty} \tan(-\theta) = -\tan\theta$$

$$\int_{0}^{\infty} \cot(-\theta) = -\cot\theta$$

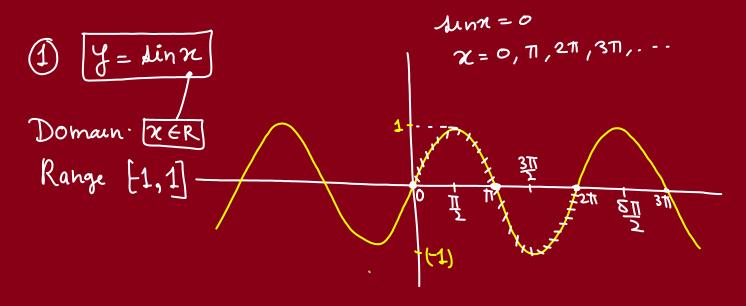
$$\int_{0}^{\infty} \cot(-\theta) = -\cos\theta$$

$$(os(-0) = cos 0)$$

$$Sec(-0) = Sec 0$$

$$Comp Sci$$

GRAPH OF TRIG FUNCTION



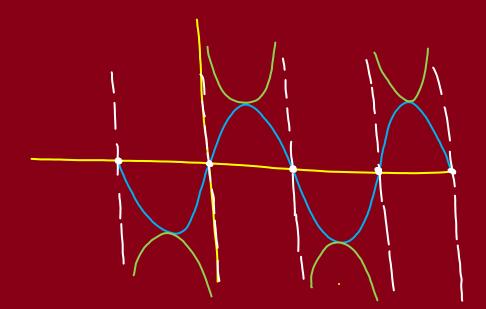
Domain: XER y = Cosx Range y ∈ [-1, 1] 34 511 (03× - 0 x= (2n+1)tT

Inc 8n 3 tann = y = sinn Cosx 70 $\chi \neq (2n+1)\pi$ Domain Sunn bost Seek 271 Range Cosecn tanz (m) Period = TI T

sun to $x \neq n\pi$ Domain R- {nπ'y Range. R

ULTI TOPI y = Secn = (orsa CO>X 70 2 7 (2n+1) IT Range: (-00,-1) U[1,00)

$$y = cosecn = \frac{1}{sim}$$
 $sinn \neq 0$ $x \neq n\pi$



Domain · R - {n11} Range · (-0, -1] U[1, 0)

COMPOUND ANGLE

Lo Add 2 or more angles (A+B)

Coso = Lin (90-0)

$$Jun(A+B) = Jun A Cos B + Cos A sin B$$

$Jun(A-B) = Jun A Cos (B) - Cos A Jun (B)$
$Cos (A+B) = Jun (90 - A - B)$
= $Jun (90-A) Cos B - Cos (90-A) Jun B$
= $Cos A Cos B - Jun A Jun B$

$$Cos(A-B) = CosA Cos(B) + Jun A Jin(B)$$

$$tan(A+B) = \frac{xin(A+B)}{Cos(A+B)} = \frac{xinA costB + CosA sinB}{CosA costB}$$
 $B \rightarrow (-B)$

CosA costB - AinA sinB

CosA costB

$$\tan(A-B) = \frac{\tan A - \tan(B)}{1 + \tan A \tan(B)}$$

$$\frac{\tan A + \tan B}{1 - \tan A \tan(B)}$$

$$\# \cot(A+B) = \frac{\cos(A+B)}{\sin(A+B)}$$

$$= \underbrace{\cot(A) \cot(-B) - 1}_{\cot(-B) + \cot A}$$

=
$$\frac{\text{Cot A cot B} + 1}{\text{Cot B} - \text{Cot A}}$$

$$tan\left(\frac{\pi}{4} + A\right) = \frac{tan\frac{\pi}{4} + tanA}{1 - tan\frac{\pi}{4}tanA}$$

$$tan(\frac{\pi}{4} + A) = \frac{1 + tanA}{1 - tanA}$$
$tan(\frac{\pi}{4} - A) = \frac{1 - tanA}{1 + tanA}$

TRANSFORMATION FORMULAS

$$0) \sin(A+B) + \sin(A-B) = 2 \sin(A) \cos(B)$$

$$\frac{C+D}{2}$$

$$(4) \log (A + B) - \cos (A - B) = -2 \sin A \sin B$$

$$A+B=C \qquad A=\frac{C+D}{2}$$

$$A-B=D$$

$$2A=C+D$$

$$2 = C+D$$

(2)
$$\sin C - \sin D = 2 \cos \left(\frac{C+D}{\lambda}\right) \sin \left(\frac{C-D}{\lambda}\right)$$

(3) $\cos C + \cos D = 2 \cos \left(\frac{C+D}{\lambda}\right) \cos \left(\frac{C-D}{\lambda}\right)$

(4)
$$\cos(-\cos b) = -2 \sin(\frac{c+b}{2}) \sin(\frac{c-b}{2})$$

$$tan(A+B) = tanA + tanB$$

 $1 - tanA tanB$

$$tan(\theta_1 + \theta_2 + ... + \theta_n) = \frac{S_1 - S_3 + S_5 \cdot ...}{1 - S_2 + S_4 - S_6 \cdot ...}$$

$$S_1 \Rightarrow tan\theta_1 + tan\theta_2 + ... + tan\theta_n$$

$$S_2 \Rightarrow \tan \theta_1 \tan \theta_2 + \tan \theta_2 \tan \theta_3 + \cdots + \tan \theta_{n_1} \tan \theta_n$$
 $S_3 \Rightarrow \cdots$

$$\tan(\theta_1 + \theta_2 + \theta_3) = \frac{S_1 - (S_3)}{1 - S_2}$$

$$= \frac{\tan \theta_1 + \tan \theta_2 + \tan \theta_3 - \tan \theta_1 \tan \theta_2 \tan \theta_3}{1 - \left(\tan \theta_1 \tan \theta_2 + \tan \theta_2 \tan \theta_3 + \tan \theta_3 + \tan \theta_3 + \tan \theta_3\right)}$$

$$Jun(2A) = Jun(A+A) = Jun A cos A + Cos A Jun A = 2 Jun A Cos A$$

1 + tan2A

$$\operatorname{din}(2A) = 2 \operatorname{din}A \operatorname{Cos}A$$
 # $\operatorname{Cos}A = \operatorname{Cos}^2A - \operatorname{din}^2A$

$$= \frac{2 \tan A}{1 + \tan^2 A}$$

$$= \frac{2 \tan A}{1 - 2 \sin^2 A}$$

$$= \frac{2 \tan A}{1 - 2 \sin^2 A}$$

$$= \frac{1 - \tan^2 A}{1 - 2 \sin^2 A}$$

$$tan 2A = \frac{lun 2A}{cos2A} = \frac{2 sun A cosA}{cos2A}$$

$$\frac{cos2A}{cos2A}$$

$$tan(2A) = \frac{2 tan A}{1 - tan^2 A}$$

1+ 682A = 268A Sin = paap

$$\cos 2A = 1 - 2\sin^2 A$$

$$2\sin^2 A = 1 - \cos 2A$$

$$1 - \cos 2\theta = 2\sin^2 \theta$$

$$1 - 6920 = 24m^20$$
 $1 + 6920 = 26920$

$$1 + \cos 2\theta = 2\cos^2 \theta$$

$\sin 3\theta = 3\sin \theta - 4\sin^3 \theta$

$$\theta = \frac{1}{2} \cos^2 \theta = \frac{1}{2} \cos^2 \theta$$

chote - bade

 $\sin \theta = \cos (90 - \theta)$ Sin15 = Cos 75 1m(H) Sin75= Co3150

(4)(<u>I</u>) sin 15° = Lun (45-30)

$$= A \ln 45 \cos 30 - \cos 45 \sin 30 \qquad |5° = \frac{\pi}{12}|$$

$$= \left(\frac{1}{12}\right) \left(\frac{13}{2}\right) - \left(\frac{1}{12}\right) \left(\frac{1}{2}\right) \qquad |75° = \frac{5\pi}{12}|$$

18, 36, 72, 54°

$$\frac{\pi}{10}$$
 $\frac{\pi}{5}$
 $\frac{3\pi}{10}$

Proof: $\Rightarrow \Theta = 18^{\circ}$

$$\Rightarrow 3\theta + 2\theta = 90$$

 \Rightarrow 50 = 90°

$$\Rightarrow 30 = 90 - 20$$

$$\Rightarrow \cos(30) = \cos(40 - 50)$$

Sin18 = Cos72"

Cos 18° = Sin 72°

din36 = cos 54

$$46030 - 36050 = 2500000$$

$$4 (68^2 0 - 3 = 2 4 400)$$

$$4\left(1-4un^2\theta\right)-3=24in\theta$$

$$4(1-4un^20)-3=24in0$$

$$4(1-440) - 3 = 24400$$

$$4 \sin^2 \theta + 24400 - 1 = 0$$

$$4 \sin^2 \theta + 24400 - 1 = 0$$

$$5 \sin^2 \theta = -2 \pm \sqrt{4 + 16} = -2 \pm 2\sqrt{5}$$

$$8$$

$$\cos 2\theta = 1 - 2 \sin^2 \theta$$

$$\cos 3\theta = 1 - 2 \sin^2 \theta$$

$$= 1 - 2 \left(\frac{\sqrt{5} - 1}{4} \right)^2$$

= 45+1

$$\sin 36^{\circ} = ?$$
 $2\sin^{2} 36 = 1 - \frac{\sqrt{5} - 1}{4}$

$$\cos 20 = 1 - 2\sin^2 0$$

$$\sin 36 = 5 - 15)(2)$$

$$22.5° = \frac{\pi}{8} = \frac{45°}{2}$$

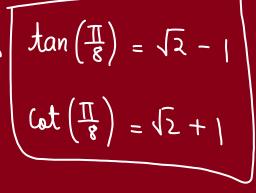
$$tan20 = 2 tan0$$

$$0 = \frac{\pi}{8}$$

$$1 = 2 tan \frac{\pi}{8}$$

$$1 - tan^2 \frac{\pi}{8}$$

$$1 - tan^2 \frac{\pi}{8} = 2 tan \frac{\pi}{8}$$



Cosine Series (Product) pacman ?

$$\cos(A) \cos 2A \cos 4A \cos 8A$$
 . $\cos(2^{n-1}A) = \frac{\sin(2^n A)}{2^n \sin A}$

- 1 product
- @ Angle -> GP (r=2)
- 3) n-s no of terms
 A First Angle | Smallest Angle

PROOF .-= 2 Aun A Cos A Cos 2 A Cos 4 A Cos 8 A 68(2ⁿ⁻¹A) 2 den A = [21112A COS2A] COS4A COS8A.. COS(2n-1A) 22 lin A Jun(2hA) 7 2n SunA

 $2^{n-1}A \times 2$ 2^nA

$$\cos \alpha + \cos (\alpha + \beta) + \cos (\alpha + 2\beta) + + \cos (\alpha + (n-1)\beta) = \frac{\sin (\frac{n\beta}{2})}{\sin (\frac{\beta}{2})} \cos (\alpha + (\frac{n-1)\beta}{2})$$

1= 0

sine series (SUM)

dinx + din(x+B) + din(x+2B) + . + din(x+(n-1)B) =
$$\frac{din(\frac{nB}{2})}{din(\frac{B}{2})}$$
 din(x+(n-1)B)

= $\frac{din(\frac{B}{2})}{din(\frac{B}{2})}$

#I SUM #2 A.P

where, n -> no of terms

$$\alpha \rightarrow First Angle$$

B-> (o mmon diff

Cosecx Ke Levies

$$= \left(\cot\left(\frac{FA}{2}\right) - \cot\left(LA\right)\right)$$

Cosecon + Cosec
$$2n$$
 + Cosec $4n$ + . + Cosec (2^nn) = $\cot(\frac{x}{2})$ - $\cot(2^nn)$

Proof:
$$T_1 = \text{Cosecn} = \frac{\sin(x - \frac{x}{2})}{\text{June } \sinh(\frac{x}{2})} = \frac{\text{June } \cos \frac{x}{2} - \cos x \cdot \tan(\frac{x}{2})}{\text{June } \sinh(\frac{x}{2})}$$

$$T_{1} = \cot(\frac{x}{2}) - \cot(n)$$

$$T_{2} = \cot(n) - \cot(2x)$$

$$T_{3} = \cot(2n) - \cot(4n)$$

$$T_{n} = \cot(x^{2}n) - \cot(2^{n}n)$$

$$T_{n} = \cot(x^{2}n) - \cot(x^{2}n)$$

$$S = \cot(x^{2}n) - \cot(x^{2}n)$$

Max and mini Value of Trigo fr: Range $\in [\alpha, \beta]$ Known trig fr Type 1 Use the Range of (osecre) (-00,-1] () (1,00) -1 < Jinx < 1 -1 < 69x < 1 tanx (R

Sin 2h | sum | \ [0,1] Sin²x } [0,1] | tam | } [0, 00) tan'x (o, ~) |secon| $(1, \infty)$ Secret
(blech) (1,00)

$$\underline{Ex}$$
 $y = 3 + \lambda unn$

[2,4]

 $\frac{\text{Type 2}}{\text{Type 2}} \quad f(n) = a \sinh n + b \cos n$

$$-\sqrt{a^2+b^2} \le a \, \text{Aunn} + b \, \cos x \le \sqrt{a^2+b^2}$$

$$-\sqrt{3^2+4^2} \le 3 \, \text{Ainn} + 4 \, \cos x \le \sqrt{3^2+4^2}$$

$$-5,5]$$

Type 3 QE in sinn or cosn'

$$f(n) = \frac{\cos 2\pi + 3 \sin n}{\sin n} \quad \text{Range of } f(n)$$

$$= 1 - 2 \sin^2 x + 3 \sin n \qquad \frac{\frac{3}{2}}{2} = (\frac{3}{4})$$

$$=-2\left(\sin^2 x - \frac{3}{2} \sin x - \frac{1}{2}\right)$$

$$= -2 \left(\frac{\sin^2 x - \frac{3}{2} \tan x + \frac{9}{16} - \frac{9}{16} - \frac{1}{2}}{\cos^2 x + \frac{3}{2} \tan x + \frac{9}{16} - \frac{9}{16} - \frac{1}{2}} \right)$$

$$f(n) = -2\left(\frac{4nn - \frac{3}{4}}{2}\right)^2 - \frac{17}{16}$$

$$f(n) = \frac{17}{8} - 2\left(\frac{4nn - \frac{3}{4}}{2}\right)^2$$

$$f(n) = \frac{17}{8} - 2\left(\frac{3}{4}\right)^2$$

$$f(n) = \frac{17}{8} - 2\left(\frac{3}{4}\right)^2 = \frac{17}{8} - \frac{49}{8} = \frac{32}{8} = \frac{32}{8} = \frac{32}{8}$$

$$max(n) = \frac{17}{8} - 0 = \frac{17}{8}$$

Type 4

$$\frac{M-1}{M-2} = \frac{a^2 \tan^2 \theta + b^2 \cot^2 \theta}{a^2 \tan^2 \theta + b^2 \cot^2 \theta} = \frac{a^2 b^2}{a^2 b^2}$$

$$\frac{M-2}{a^2 \tan^2 \theta + b^2 \cot^2 \theta} = \frac{a^2 b^2}{a^2 b^2} = \frac{a^2 b^2}{a$$



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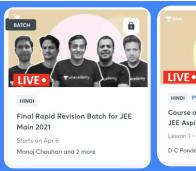
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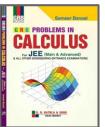


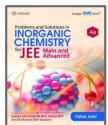




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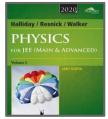


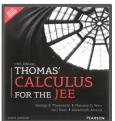








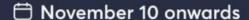






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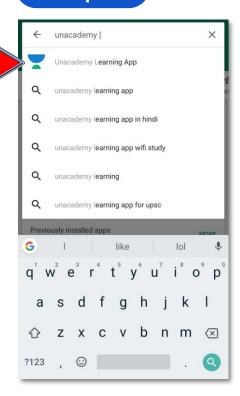


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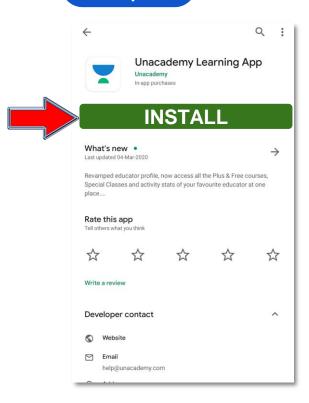
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Step 1

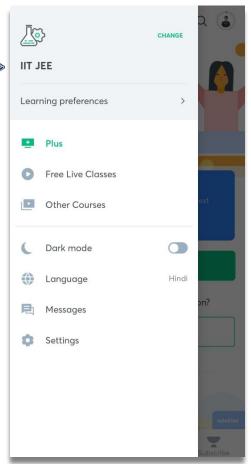


Step 2



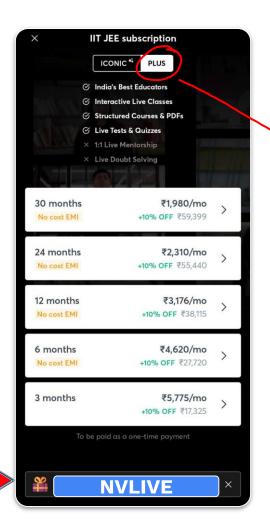






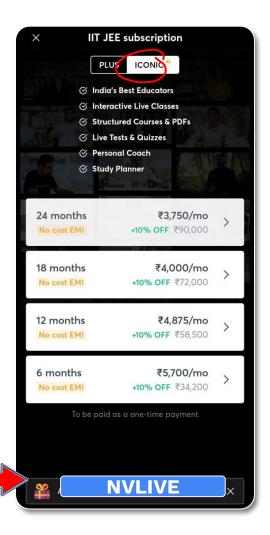






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