

# (CURRENT ELECTRICITY)

①

(CHAPTER-3)

## ELECTRIC CURRENT (I)

It is defined as rate of flow of electric charge through any cross section of a conductor.

$$I = \frac{\text{total charge}}{\text{time taken}}$$
$$I = \frac{q}{t} = \frac{ne}{t}$$
$$I = \lim_{\Delta t \rightarrow 0} \frac{\Delta q}{\Delta t} = \frac{dq}{dt}$$

→ Scalar quantity

SI unit → A

CGS unit → st A

## CURRENT DENSITY (J):-

It is the ratio of the current at that point in the conductor to the area of the cross section of the conductor at that point.

$$J = \frac{I}{A}$$

$$I = JA$$

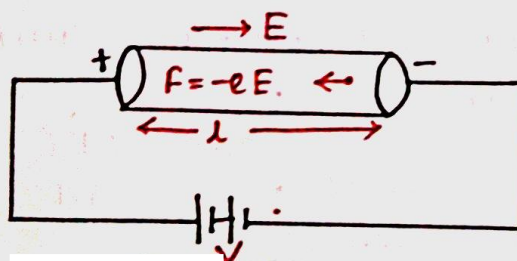
$$\Rightarrow \boxed{I = \vec{J} \cdot \vec{A}}$$

→ Vector quantity.

## DRIFT VELOCITY ( $v_d$ )

It is defined as avg. velocity gained by the free  $e^-$ s of a conductor in the opposite direction of the externally applied electric field.

## DRIFT OF ELECTRONS:-



If  $\vec{v}_1, \vec{v}_2, \dots, \vec{v}_N$  be the velocities of N no of free electrons,

Then, avg velocities of electrons =  $\frac{\vec{v}_1 + \vec{v}_2 + \dots + \vec{v}_N}{N} = 0$

Thus, there is no net flow of charge in any direction. In the presence of electric field, each  $e^-$  experiences a force,  $\vec{F} = -e\vec{E}$

The negative sign indicate  $e^-$  are moving in the opp direction of  $\vec{E}$ .

$$\begin{aligned} \vec{F} &= -e\vec{E} \\ \Rightarrow m\vec{a} &= -e\vec{E} \\ \Rightarrow \vec{a} &= \frac{-e\vec{E}}{m}, \quad m = \text{mass of the electron.} \end{aligned}$$

If n, no of  $e^-$  gain velocity component

$$\vec{v}_1, \vec{v}_2, \dots, \vec{v}_n$$

$$\vec{v}_1 = \vec{u}_1 + \vec{a}t_1$$

$$\vec{v}_2 = \vec{u}_2 + \vec{a}t_2$$

⋮

$$\vec{v}_n = \vec{u}_n + \vec{a}t_n$$

$$\vec{u}_1 + \vec{u}_2 + \dots + \vec{u}_n = \vec{u}_1 + \vec{u}_2 + \dots + \vec{u}_n + \vec{a}(t_1 + t_2 + \dots + t_n)$$

$$\Rightarrow \frac{\vec{v}_1 + \vec{v}_2 + \dots + \vec{v}_n}{n} = \frac{\vec{u}_1 + \vec{u}_2 + \dots + \vec{u}_n}{n} + \frac{\vec{a}(t_1 + t_2 + \dots + t_n)}{n}$$

$$\Rightarrow \vec{v}_d = \vec{a}\tau, \quad \begin{aligned} v_d &= \text{drift velocity} \\ \tau &= \text{relaxation time.} \end{aligned}$$

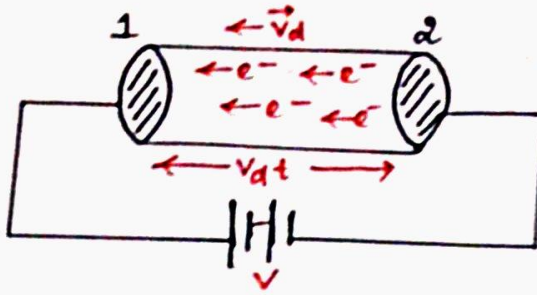
$\tau$  is the avg. time elapsed between 2 successive collision of the electron.

$$\vec{v}_d = \frac{-e\vec{E}\tau}{m}$$



## RELATION BETWEEN ELECTRIC CURRENT AND DRIFT VELOCITY :-

3



$A$  = area of the cross-section  
 $n$  = full electron density  
 $t$  = time taken by electron to move from cross-section 1 to 2.

distance bet<sup>n</sup> two cross-section =  $v_d t$

Volume bounded by two cross-section =  $Al = Av_d t$

no. of electrons in that volume =  $nAv_d t$

no. of electron passes through the cross-section 1 in time  $t = nAv_d t$

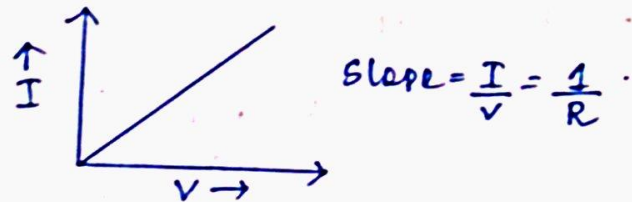
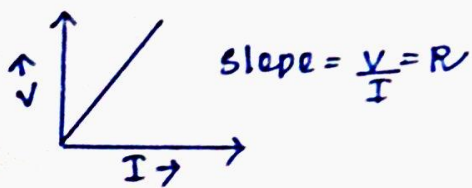
$$I = \frac{q}{t} = \frac{nAv_d t \cdot e}{t} = neAv_d$$

$$I = neAv_d$$

OHM'S LAW:- The potential difference between two ends of a conductor is directly proportional to current passing through it at constant temperature.

$$V \propto I$$

$$\Rightarrow V = IR$$



DEDUCTION OF OHM'S LAW:-

$$I = neAv_d$$

$$= neA \left( \frac{eV\tau}{m\lambda} \right) = \left( \frac{ne^2 A \tau}{m\lambda} \right) V$$

$$V = \left( \frac{m\lambda}{ne^2 \tau} \right) I$$

$$\Rightarrow V = RI$$

$$\Rightarrow V \propto I$$

$R = \frac{m\lambda}{ne^2 \tau}$ , constant for a particular conductor at constant temp.

### LIMITATIONS OF OHM'S LAW:-

- ① only valid at constant temp.
- ② some substances do not obey ohm's law.

4

### VECTOR FORM OF OHM'S LAW:-

$$\begin{aligned} J &= \frac{I}{A} \\ &= \frac{neAv_d}{A} \\ &= n \cdot \frac{eE\tau}{m} \cdot e \\ &= \left( \frac{ne^2\tau}{m} \right) E \end{aligned}$$

$$J = \sigma E$$

In vector form.

$$\vec{J} = \sigma \vec{E}$$

RESISTANCE (R):- It is defined as the opposition offered to the flow of current

SI unit  $\rightarrow \Omega$

CGS unit  $\rightarrow \text{st } \Omega / \text{ab } \Omega$

$$R = \frac{ml}{nAe^2\tau}$$

Resistance depends on:-

- ① Geometry of conductor
- ② Nature of material
- ③ Temperature.

CONDUCTANCE (G):- It is defined as the reciprocal of resistance.

$$G = \frac{1}{R} = \frac{nAe^2\tau}{ml}$$

SI unit.-  $\Omega^{-1}$

RESISTIVITY ( $\rho$ ):

$$R = \frac{m l}{n A e^2 \tau}$$

$$= \left( \frac{m}{n e^2 \tau} \right) \frac{l}{A}$$

$$\Rightarrow R = \rho \frac{l}{A} \text{ where } \rho = \frac{m}{n e^2 \tau} \text{, which is constant for a particular material at constant temp.}$$

DEFINITION OF  $\rho$ :-  $\rho = \frac{RA}{L}$  ,  $A = 1 \text{ m}^2$  ,  $L = 1 \text{ m}$  ,  $\rho = R$

It is defined as resistance of a rod of that material of length 1m and area of cross section  $1 \text{ m}^2$ .

SI unit  $\rightarrow \Omega \text{ m}$

$$R = \frac{\rho L}{A} \text{ , } R \propto L \text{ (A is constant)}$$

$$R \propto \frac{1}{A} \text{ (L is constant)}$$

SPECIAL CASE:-CASE-I

When  $A$  is not constant

$$R = \rho \frac{l}{A} \times \frac{l}{l}$$

$$= \frac{\rho l^2}{\text{Vol}}$$

$$\Rightarrow R \propto l^2$$

CASE-II

when  $l$  is not constant

$$R = \rho \frac{l}{A} \times \frac{A}{A} = \frac{\rho l A}{A^2}$$

$$= \frac{\rho \times \text{Vol}}{A^2}$$

$$\Rightarrow R \propto \frac{l}{A^2}$$

CONDUCTIVITY ( $\sigma$ ):

It is defined as reciprocal of resistivity

$$\sigma = \frac{1}{\rho} = \frac{n e^2 \tau}{m}$$

SI unit:-  $\Omega^{-1} \text{ m}^{-1}$



## MOBILITY ( $\mu$ )

Mobility of a charge is defined as drift velocity per unit electric field.

$$\mu = \frac{v_d}{E}$$

$$\mu = \frac{eE\tau}{m} \times \frac{1}{E}$$

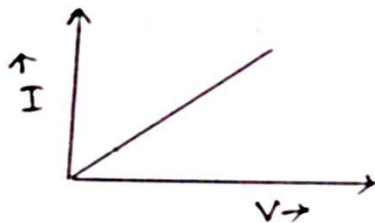
$$\mu = \frac{e\tau}{m} \quad (\text{for electron})$$

$$\mu = \frac{q\tau}{m} \quad (\text{general})$$

\* For a particular charge,  $\mu \propto \tau \propto \frac{1}{\text{temp}}$ .

\* At constant temperature,  $\mu \propto \frac{q\tau}{m}$ .

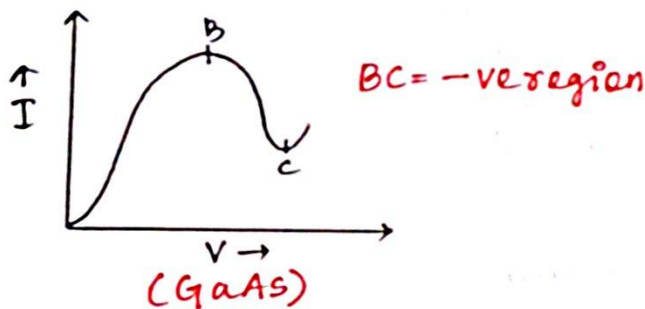
OHMIC SUBSTANCE:- Substance which obeys ohm's law.



eg:- all metals carrying low current.

NON-OHMIC SUBSTANCE:- Substance which doesn't obey ohm's law.

eg:- dil  $H_2SO_4$ , water voltameter, vacuum diode, GaAs



TEMPERATURE DEPENDANCE OF RESISTIVITY:-

$\rho_0$   $\rightarrow$  initial resistivity at temp  $T_0$

$\rho$   $\rightarrow$  final resistivity at temp  $T$

$\rho - \rho_0$   $\rightarrow$  change in resistivity.

$$\Rightarrow \rho - \rho_0 \propto (T - T_0)$$

$$\Rightarrow \rho - \rho_0 \propto \rho_0$$

$$\Rightarrow \rho - \rho_0 \propto \rho_0 (T - T_0)$$

$$\Rightarrow \rho - \rho_0 = \alpha \rho_0 (T - T_0) \quad , \quad \alpha = \text{temp. coefficient of resistivity.}$$

$$\Rightarrow \alpha = \frac{\rho - \rho_0}{\rho_0 (T - T_0)}$$

It is defined as the ratio between change in resistivity per original resistivity for degree rise of temp.

SI unit  $\rightarrow K^{-1}$

**CONDUCTOR:-** for conductor,  $\alpha = +ve$  i.e.  $\rho$  increases with  $\uparrow$  in temp.

Cause:- When temp  $\uparrow$ , K.E of free  $e^-$   $\uparrow$  so no of collision per sec  $\uparrow$ .  
- Hence, resistivity  $\uparrow$ .

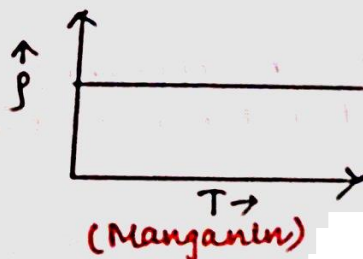
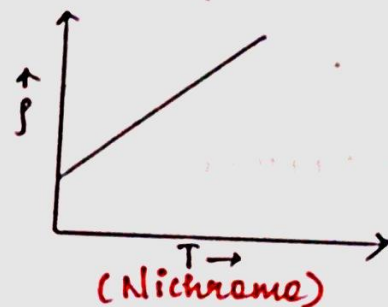
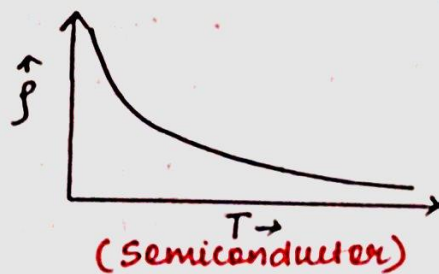
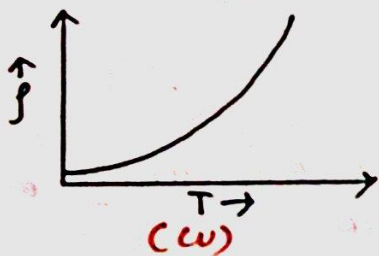
**SEMICONDUCTOR:-**  $\alpha = -ve$ , with  $\uparrow$  in temp,  $\rho \downarrow$

Cause:- When temp  $\uparrow$ , charge carrier density  $\uparrow$  sees which dominates the effect of  $Z$ .

$$\text{As } \rho = \frac{m}{ne^2Z} \quad , \quad \text{so } \rho \text{ decreases.}$$

**INSULATOR:-**  $\alpha = -ve$ ,  $\rho \downarrow$  sees with temperature.

**$\rho \sim T$  GRAPHS:-**



USE OF ALLOY IN MAKING RESISTOR:-

- ①  $\rho$  of alloy is very high
- ② They have very small temp. of coefficient.
- ③ least affected by atmospheric conditions such as air, moisture, pressure.

COLOUR CODE OF CARBON RESISTOR:-

- B  $\longrightarrow$  Black  $\longrightarrow$  0
- B  $\longrightarrow$  Brown  $\longrightarrow$  1
- R  $\longrightarrow$  Red  $\longrightarrow$  2
- O  $\longrightarrow$  Orange  $\longrightarrow$  3
- Y  $\longrightarrow$  Yellow  $\longrightarrow$  4
- G  $\longrightarrow$  Green  $\longrightarrow$  5
- B  $\longrightarrow$  Blue  $\longrightarrow$  6
- V  $\longrightarrow$  Violet  $\longrightarrow$  7
- G  $\longrightarrow$  Grey  $\longrightarrow$  8
- W  $\longrightarrow$  White  $\longrightarrow$  9
- G  $\longrightarrow$  Gold  $\longrightarrow$  5%
- S  $\longrightarrow$  Silver  $\longrightarrow$  10%
- N  $\longrightarrow$  No colour  $\longrightarrow$  20%

} Tolerance

TRICK TO REMEMBER:- B B ROY of Great Britain had a Very Good Wife  
Wearing Gold & Silver Necklace.

INTERNAL RESISTANCE ( $r$ ):- The opposition offered by electrolyte due to flow of electric current is called internal resistance.

CAUSE:- Due to collision of ions.



9

- It depends on
- (1) nature of electrolyte and electrode
  - (2) area of electrode dipped in electrolyte.  
(more is the area, less is the internal resistance)
  - (3) distance between the two electrodes  
(more is the separation, more is the internal resistance)
  - (4) temperature  
(when temp ↑, internal resistance ↓ because viscosity decreases)

RELATION BETWEEN EMF AND POTENTIAL DIFFERENCE:-

(A) DISCHARGING CONDITION

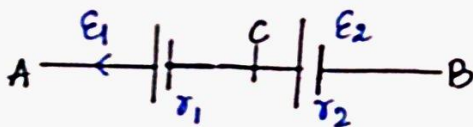
$$E = V + Ir$$

(B) CHARGING CONDITION

$$V = E + Ir$$

COMBINATION OF CELL:-

(A) SERIES



for cell 1,  $V_{AC} = E_1 - Ir_1$   
 $\Rightarrow V_A - V_C = E_1 - Ir_1$  — (1)

for cell 2,  $V_{CB} = E_2 - Ir_2$   
 $\Rightarrow V_C - V_B = E_2 - Ir_2$  — (2)

Adding (1) & (2),

$$V_A - V_B = E_1 + E_2 - I(r_1 + r_2)$$
 — (3)

for the combination,

$$V_{AB} = E - Ir$$

$$\Rightarrow V_A - V_B = E - Ir$$
 — (4)

From eqn (3) & (4),

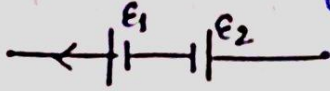
$$E_1 + E_2 - I(r_1 + r_2) = E - Ir$$

$$\Rightarrow E = E_1 + E_2$$

$$r = r_1 + r_2$$

### SPECIAL CASE:-

If the connection is wrong

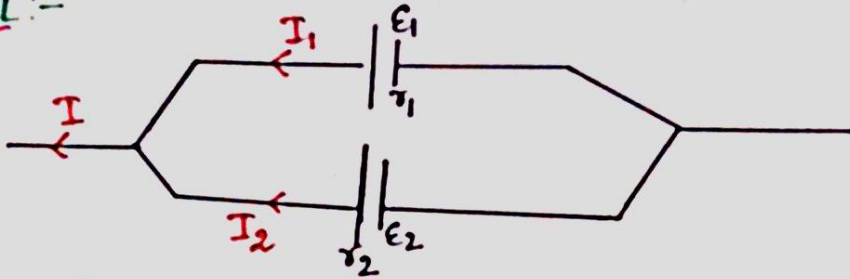


$$\boxed{E = E_1 - E_2} \quad (\text{If } E_1 > E_2)$$

$$\boxed{r = r_1 + r_2}$$

10

### (B) PARALLEL:-



for cell 1,  $V = E_1 - I r_1 \Rightarrow I_1 = \frac{E_1 - V}{r_1}$  — (1)

for cell 2,  $I_2 = \frac{E_2 - V}{r_2}$  — (2)

Similarly for the combination,

$$I = \frac{E - V}{r} \text{ — (3)}$$

$$I = I_1 + I_2$$

$$\Rightarrow \frac{E - V}{r} = \frac{E_1 - V}{r_1} + \frac{E_2 - V}{r_2}$$

$$\Rightarrow \frac{E}{r} - \frac{V}{r} = \frac{E_1 - V}{r_1} + \frac{E_2 - V}{r_2} \Rightarrow \frac{E}{r} - \frac{V}{r} = \left( \frac{E_1}{r_1} + \frac{E_2}{r_2} \right) - V \left( \frac{1}{r_1} + \frac{1}{r_2} \right)$$

Comparing both sides,

$$\frac{E}{r} = \frac{E_1}{r_1} + \frac{E_2}{r_2} \quad \& \quad \frac{1}{r} = \frac{1}{r_1} + \frac{1}{r_2} = \frac{r_1 + r_2}{r_1 r_2} \Rightarrow r = \frac{r_1 r_2}{r_1 + r_2}$$

$$= \frac{E_1 r_2 + E_2 r_1}{r_1 r_2} \cdot r = \frac{E_1 r_2 + E_2 r_1}{r_1 r_2} \cdot \frac{r_1 r_2}{r_1 + r_2}$$

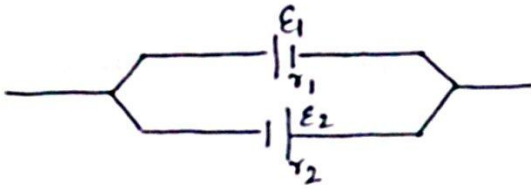
$$\boxed{E = \frac{E_1 r_2 + E_2 r_1}{r_1 + r_2}}$$



SPECIAL CASE:-

CASE-I

If connection is wrong



$$E = \frac{E_1 r_2 - E_2 r_1}{r_1 + r_2}$$

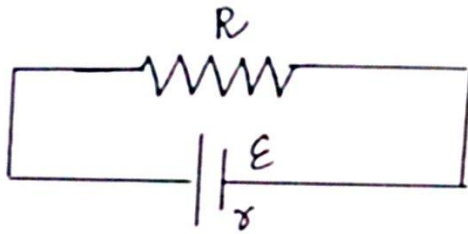
CASE-II :-

If  $E_1 = E_2 = E$

$r_1 = r_2 = r$

$$E_{net} = E$$

EXPRESSION OF CURRENT:-



$$E = V + I r$$

$$\Rightarrow E = I R + I r$$

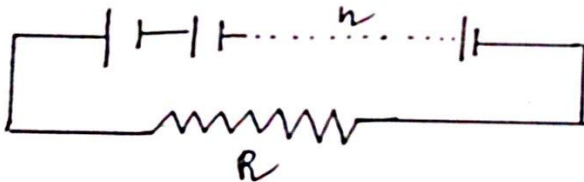
$$\Rightarrow E = I (R + r)$$

$$\Rightarrow I = \frac{E}{R + r}$$

$$I = \frac{\text{net emf}}{\text{net resistance}}$$

COMBINATION OF IDENTICAL CELL:-

(A) SERIES COMBINATION:-



$n$  = no. of cells connected in series  
 net emf =  $nE$

$$I = \frac{nE}{nr + R} = \frac{nE}{nr + R} = \frac{nE}{nr + R}$$

### CASE-I

If  $R \gg nr$

$$I = \frac{nE}{R}$$

Current depends on no. of cells.

### CASE-II

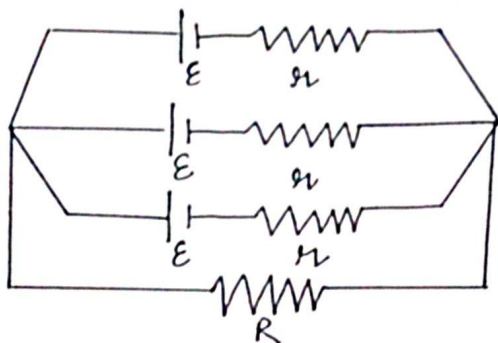
If  $R \ll nr$

$$I = \frac{E}{r}$$

Series connection is useful when external resistance is very large.

(12)

### (B) PARALLEL COMBINATION:-



$$\text{Total emf} = E$$

$$\text{Net internal resistance} = r/n$$

$$\text{Net resistance of entire network} = R + \frac{r}{n}$$

$$I = \frac{E}{R + \frac{r}{n}} = \frac{nE}{nR + r}$$

### CASE-I

If  $R \gg r/n$ ,  $r$  can be neglected

$$I = \frac{nE}{nR} = \frac{E}{R}$$

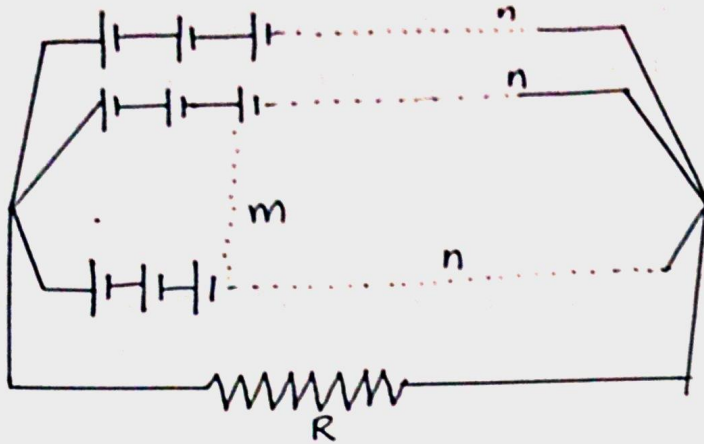
### CASE-II

If  $R \ll r/n$ ,  $R$  can be neglected

$$I = \frac{nE}{r} = n \left( \frac{E}{r} \right)$$

### MIXED CONNECTION:-





$n$  = no. of cells in each row  
 $m$  = no. of such rows

$$\text{Net emf} = nE$$

$$\text{Net internal resistance} = \frac{1}{R'} = \frac{1}{nr} + \frac{1}{nr} + \dots + m = \frac{m}{nr}$$

$$R' = \frac{nr}{m}$$

$$I = \frac{nE}{R + \frac{nr}{m}} = \frac{mnE}{Rm + nr}$$

$$mR + nr = (\sqrt{mR})^2 + (\sqrt{nr})^2 = (\sqrt{mR} - \sqrt{nr})^2 + 2\sqrt{mnRr}$$

Current will be max. when  $\sqrt{mR} = \sqrt{nr}$

$$\Rightarrow mR = nr$$

$$\Rightarrow \boxed{R = \frac{nr}{m}}$$

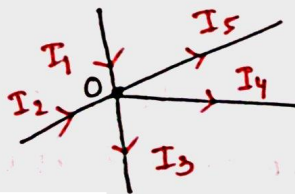
$\Rightarrow$  Total external resistance = Total internal resistance.

### KIRCHHOFF'S LAWS:-

#### (a) KIRCHHOFF CURRENT LAW / JUNCTION LAW:-

It states that algebraic sum of currents meeting at a junction is zero.

$$\boxed{\sum I = 0}$$



The current coming towards the junction is taken as +ve.  
The current going away from the junction is taken as -ve.

$$\rightarrow I_1 + I_2 - I_3 - I_4 - I_5 = 0$$
$$\rightarrow \boxed{I_1 + I_2 = I_3 + I_4 + I_5}$$

So, net current coming towards the junction = net current going out of the junction.

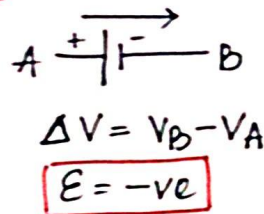
(b) KVL / loop law :-

It states that the algebraic sum of potential differences across cells and resistors in a close loop is 0.

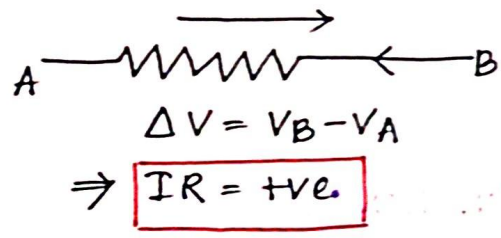
$$\boxed{\sum \Delta V = 0}$$

SIGN CONVENTION:-

① If one moves from +ve to -ve of a cell, then emf is -ve



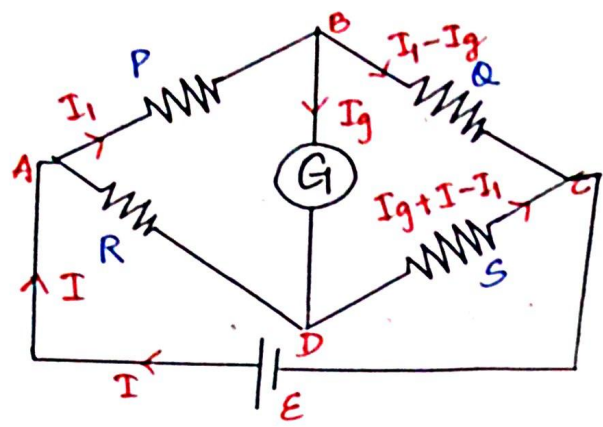
② If one moves opposite to direction of current then the product of current and resistance (IR) is taken as +ve.



WHEATSTONE BRIDGE:-

P, Q, R, S are the 4 resistors connected in wheatstone bridge.  
G → resistance of galvanometer.





Using KVL,

ABDA

$$-PI_1 - GI_5 + R(I - I_1) = 0$$

$$-I_1P - I_5G + (I - I_1)R = 0 \text{ --- (I)}$$

BCDB

$$-Q(I_2 - I_5) + S(I - I_1 + I_5) + GI_5 = 0 \text{ --- (II)}$$

The bridge is said to be balanced when no current passes through galvanometer  
i.e.  $I_5 = 0$

eqn (I) & (II) becomes,

$$-I_1P + (I - I_1)R = 0$$

$$\boxed{(I - I_1)R = I_1P} \text{ --- (III)}$$

$$-QI_2 + SI - SI_1 = 0$$

$$\boxed{I_1Q = (I - I_1)S} \text{ --- (IV)}$$

Dividing (III) & (IV),

$$\boxed{\frac{P}{Q} = \frac{R}{S}}$$

It is the balanced condition of wheatstone bridge.

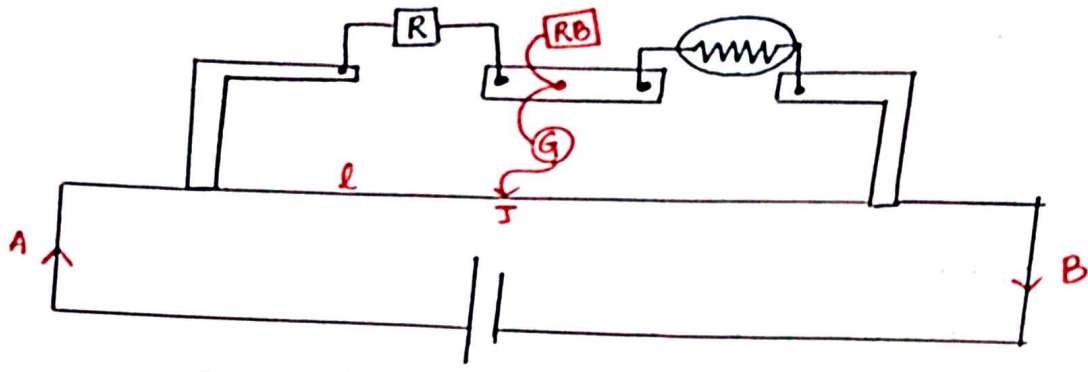
Q:- What happens to the balanced condition if cell & galvanometer are interchanged?

No change.

### METER BRIDGE :-

It is an electrical device used to measure unknown resistance.

PRINCIPLE :- It works on the balanced condition of wheatstone bridge.



R = known resistance from resistance box

S = unknown resistance

J = null point such that AJ = l

According to balanced condition of wheatstone bridge.

$$\frac{R}{S} = \frac{RAJ}{SBJ}$$

$$\Rightarrow \frac{R}{S} = \frac{l}{100-l}$$

$$\Rightarrow S = \frac{R(100-l)}{l}$$

Q :- When is metre bridge most sensitive?

If it is obtained at the middle of the wire

Q :- Why thick copper strips are used?

Because of negligible resistance

Q :- What happens to balancing length if resistance R increases?  
Increases.

### POTENTIOMETER

It is an electrical device which is used to measure emf of a cell.

PRINCIPLE OF POTENTIOMETER:-

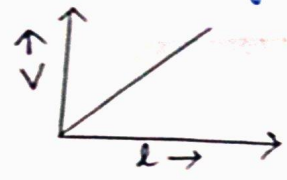
$$V = IR$$

$$\Rightarrow V = I \cdot l / A$$

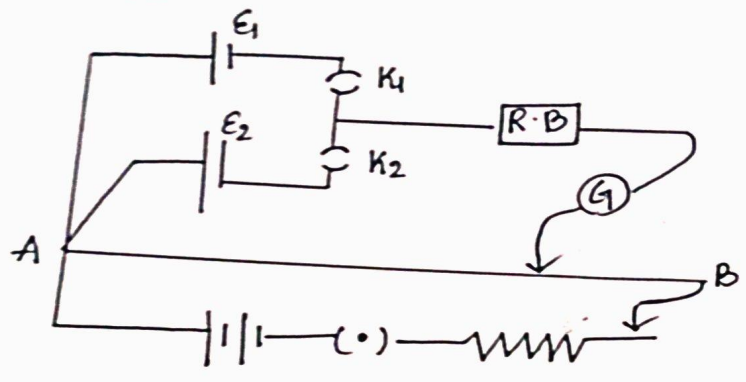
$$\Rightarrow V = \left( \frac{I \cdot l}{A} \right) l$$

$$\Rightarrow \boxed{V = Kl} , K = SI/A$$

The principle is that when a constant current flows through a wire of uniform cross-section and composition, the potential drop across any length of the wire is directly proportional to that length.



① Comparison of emf:-



- $E_1$  &  $E_2$  → are two primary cells
- $K_1$  &  $K_2$  → Two way key
- $R.B$  → Resistance box
- $E$  → Driving cell
- $K$  → Key of Auxillary / primary circuit
- $R$  → Rheostat
- $AB$  → potentiometer wire

Close  $K_1$ ,  $K_2$  is open

$$E_1 \propto l_1$$

$$\Rightarrow E_1 = Kl_1 \text{ --- (I)}$$

Close  $K_2$ ,  $K_1$  is open.

$$E_2 \propto l_2$$

$$\Rightarrow E_2 = Kl_2 \text{ --- (II)}$$

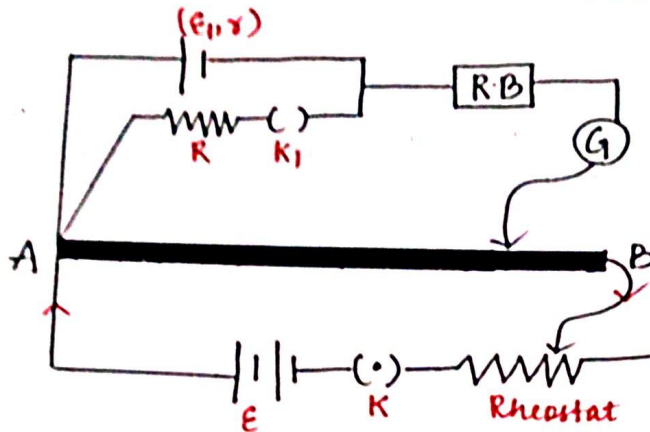


Eqn ① by Eqn ②,

$$\frac{E_1}{E_2} = \frac{l_1}{l_2}$$

18

② DETERMINATION OF INTERNAL RESISTANCE OF GIVEN PRIMARY CELL:-



CASE-I

$K_1$  is open

$$E_1 \propto l_1 \Rightarrow E_1 = K l_1 \quad \text{--- ①}$$

CASE-II

$V_1$  is closed.

$$V \propto l_2 \Rightarrow V = K l_2 \quad \text{--- ②}$$

$$\frac{\text{eqn ①}}{\text{eqn ②}} = \frac{E_1}{V} = \frac{l_1}{l_2}$$

$$\Rightarrow \frac{I(R+r)}{IR} = \frac{l_1}{l_2}$$

$$\Rightarrow 1 + \frac{r}{R} = \frac{l_1}{l_2}$$

$$\Rightarrow \frac{r}{R} = \frac{l_1}{l_2} - 1$$

$$\Rightarrow r = \left( \frac{l_1 - l_2}{l_2} \right) R$$

$l_1$  = balancing length when only  $E_1$  is connected

$l_2$  = balancing length when  $R$  is connected